

An Application of Secure Computation to Tagiron

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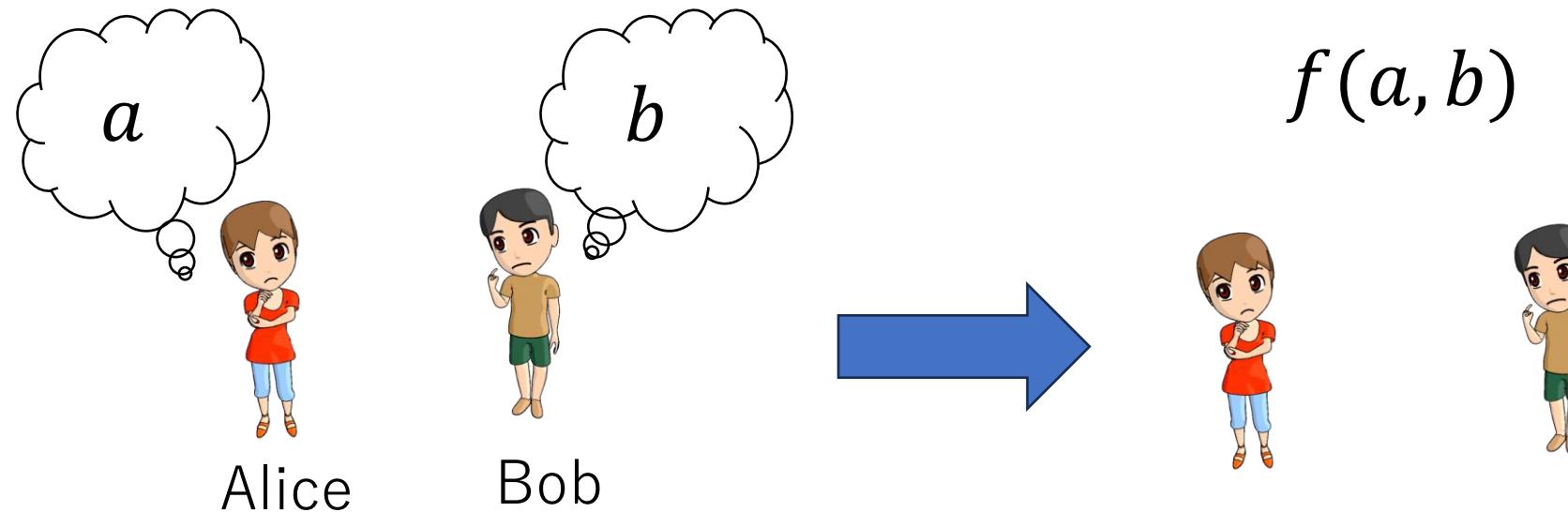
An Application of Secure Computation to *Tagiron*

A logic-based deduction game



Tagiron by JELLY JELLY GAMES (<https://jelly2games.com/tagiron>)

An Application of *Secure Computation* to Tagiron



Cryptographic technique enabling players to know only the value of a function without leaking information about inputs

An *Application* of Secure Computation to Tagiron

We apply secure computation to enhancing gameplay of Tagiron.

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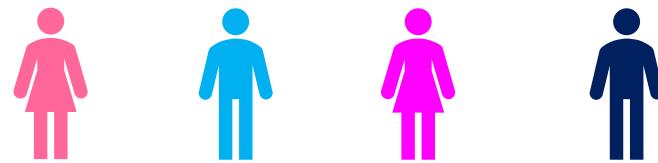
3. Preprocessing Protocol

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Tagiron (a.k.a. Break the Code)

- A popular logic-based deduction game invented by Ryohei Kurahashi.
- The game is played with 2 to 4 players, but we focus on the *4-player* version.



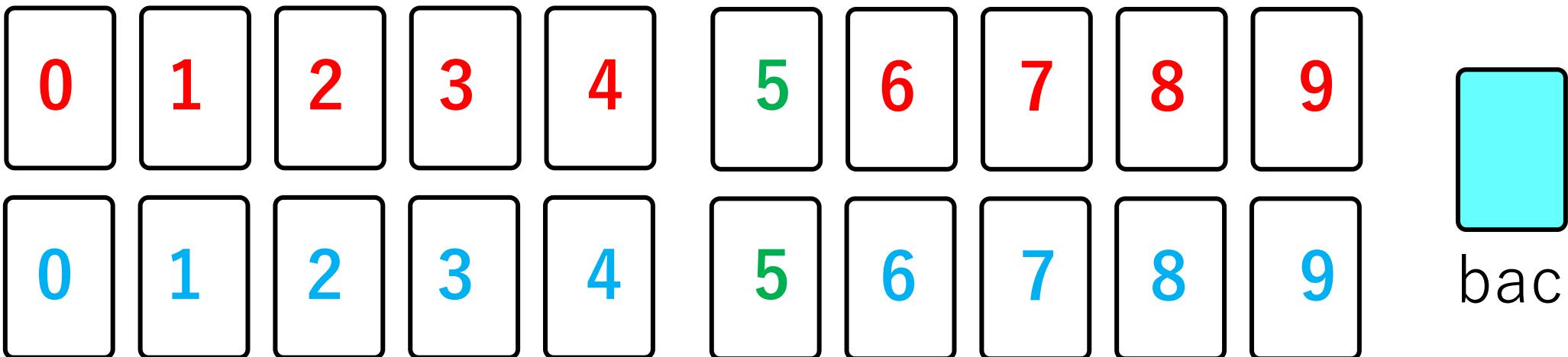
- There are 20 Tagiron cards (small tiles).



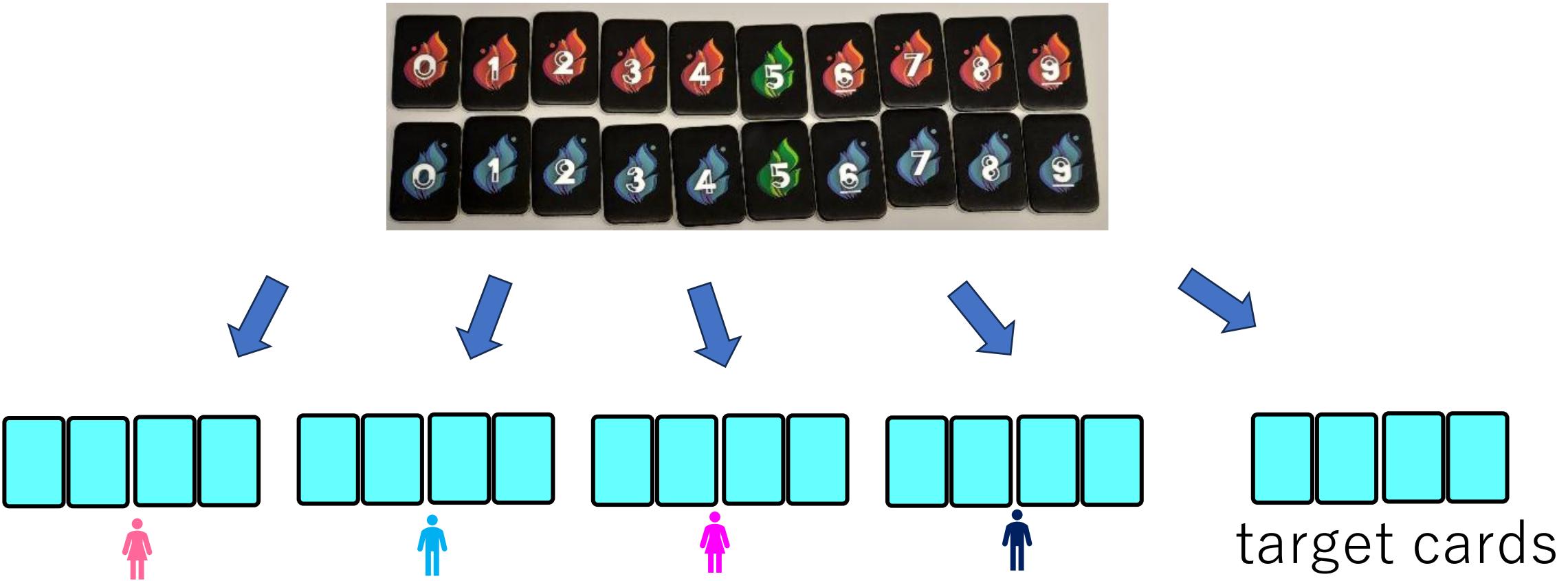
20 Tagiron cards (small tiles)



- Has a number from 0 to 9 and a color of red, blue, or green

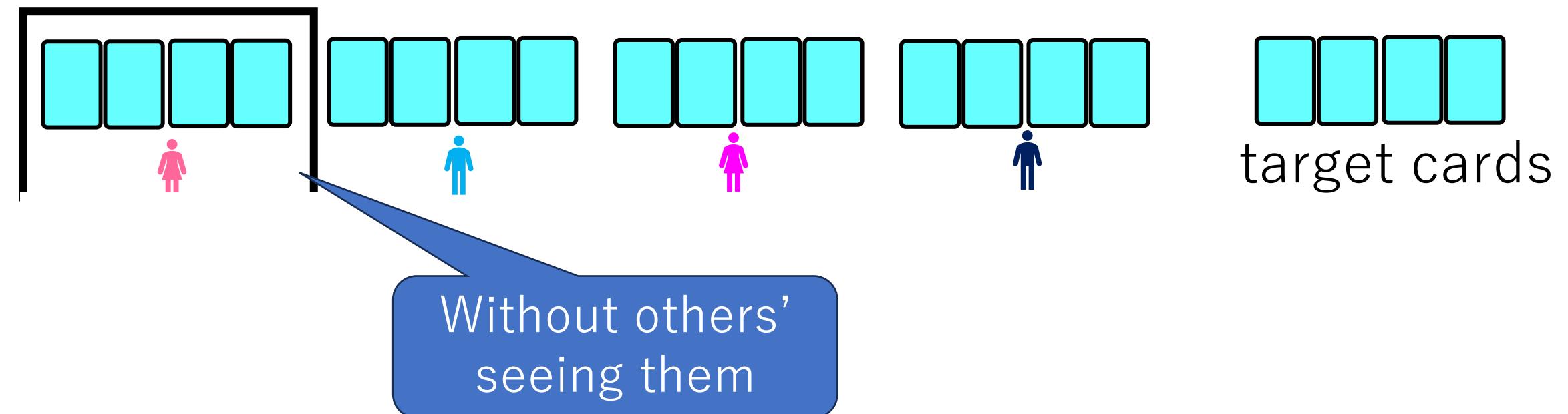


The 20 Tagiron cards are shuffled and distributed:

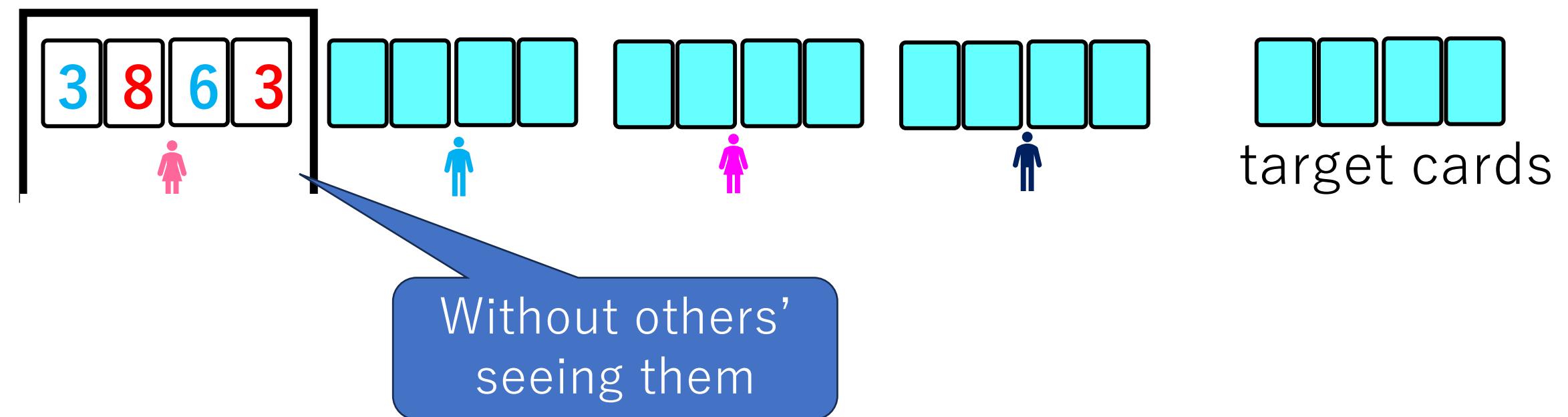


- Each player receives 4 cards.
- The remaining 4 cards become the target to deduce.

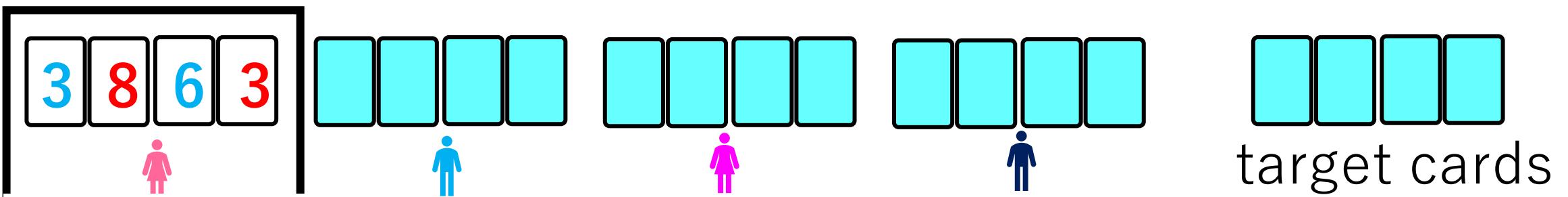
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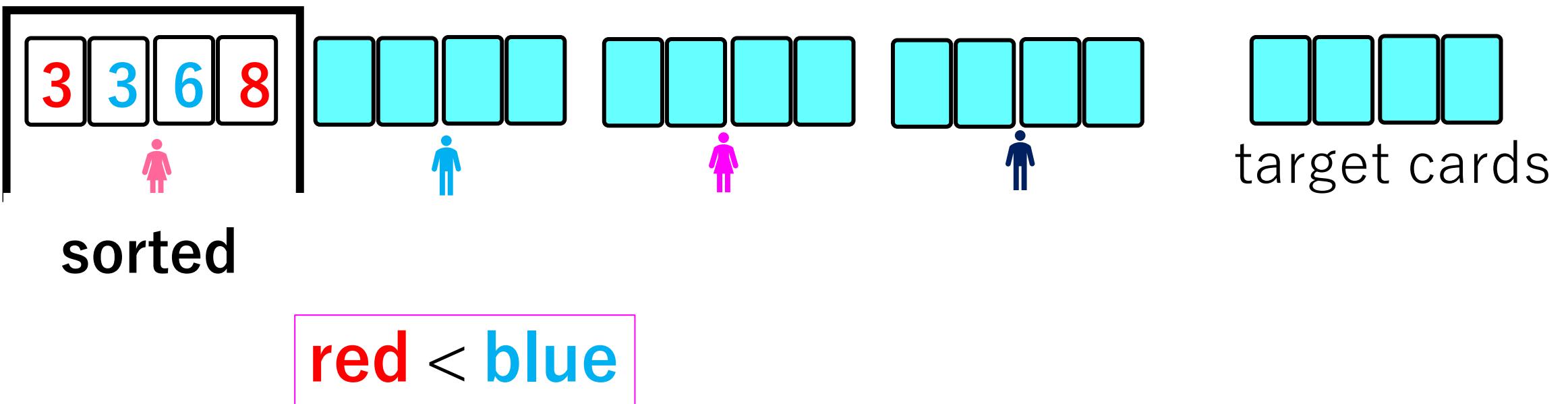


- Each player secretly looks at their 4 cards
- Sort the 4 cards in ascending order from left to right

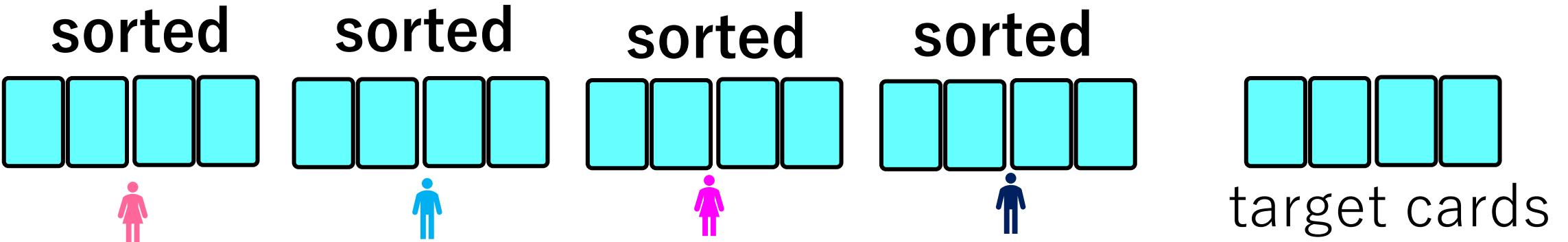


red < blue

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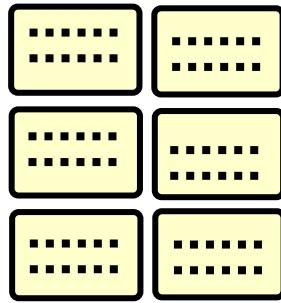


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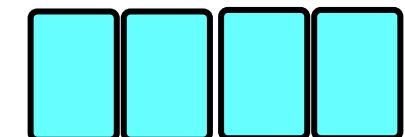
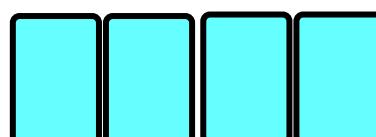
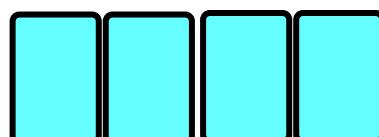
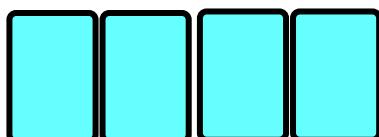
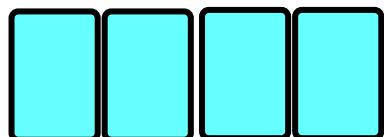


red < blue

19 **question cards** are shuffled and 6 of them are revealed



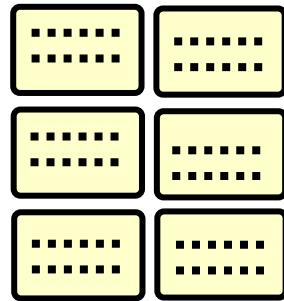
“Where is 9?”
“How many blue numbers?”
“How many odd numbers?”
and so on.



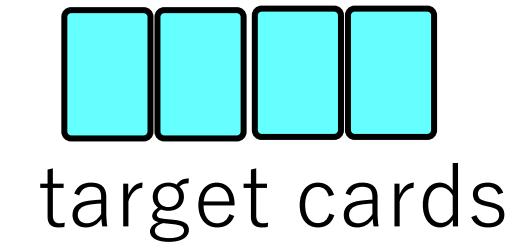
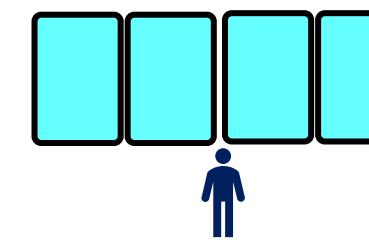
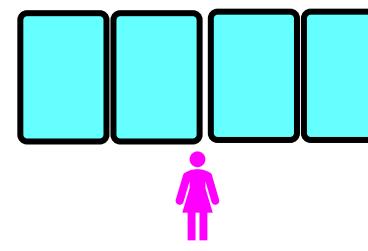
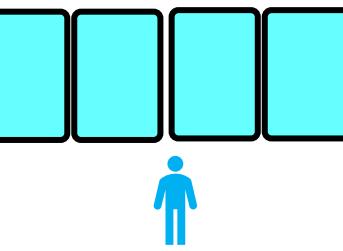
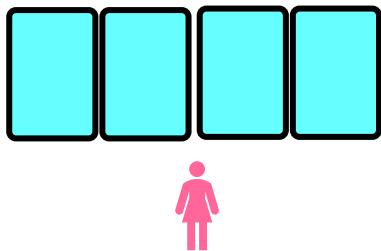
target cards

Players take turns:

1. A player chooses one question card and asks a question.
2. All players answer the question honestly.
3. A new question card is revealed from the deck.

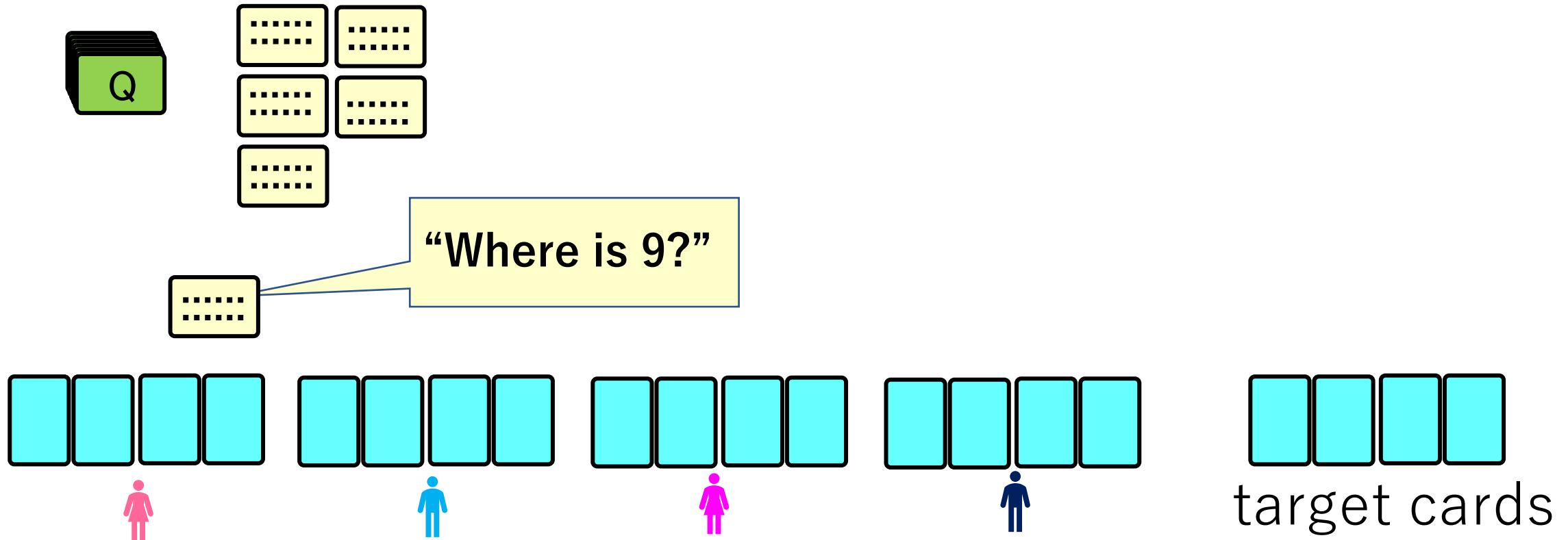


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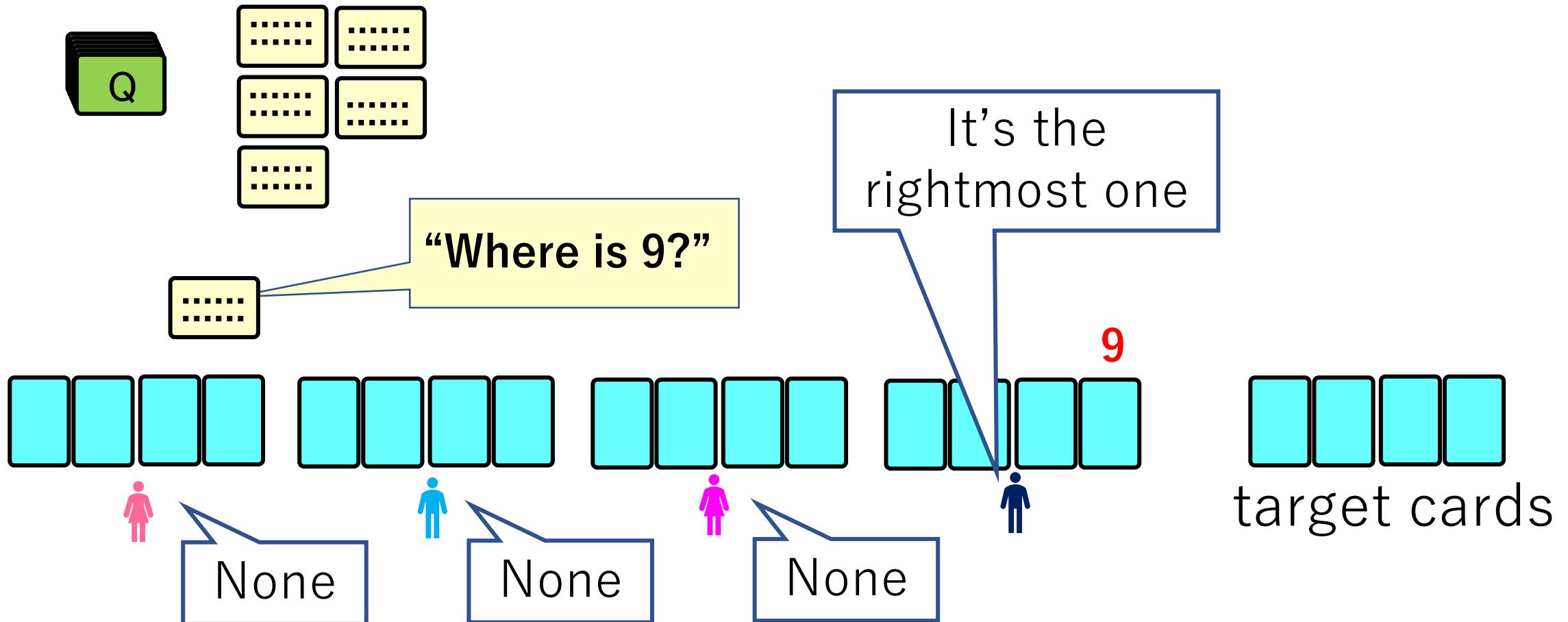
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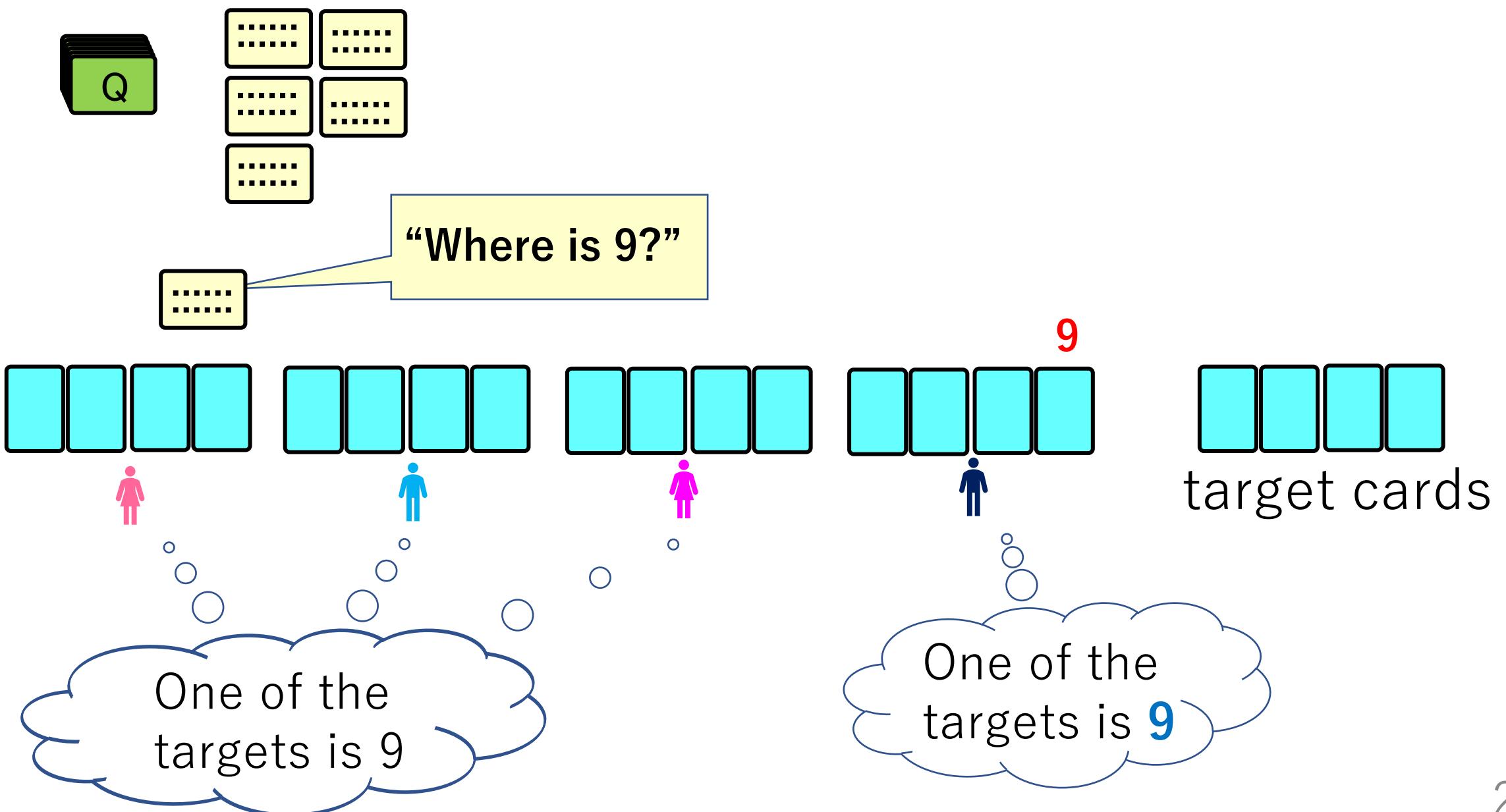
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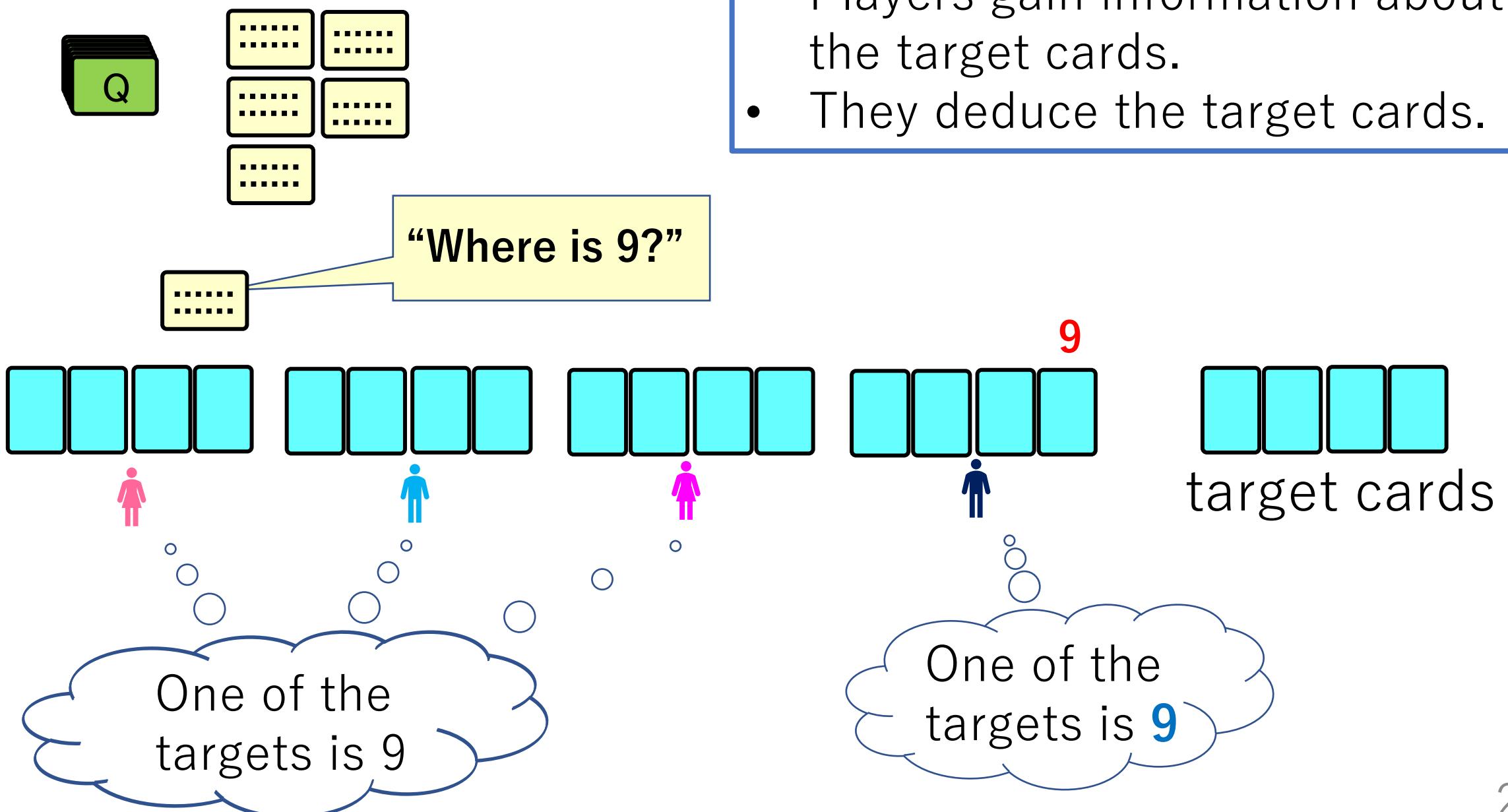


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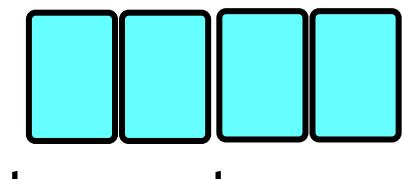
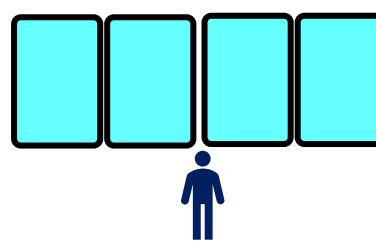
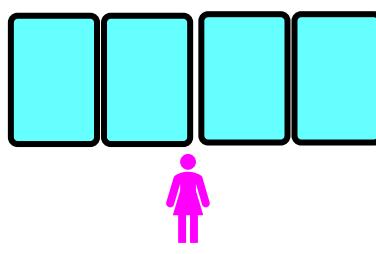
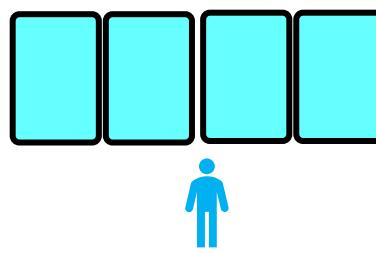
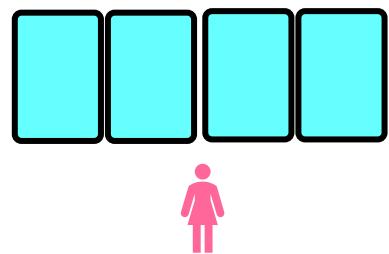
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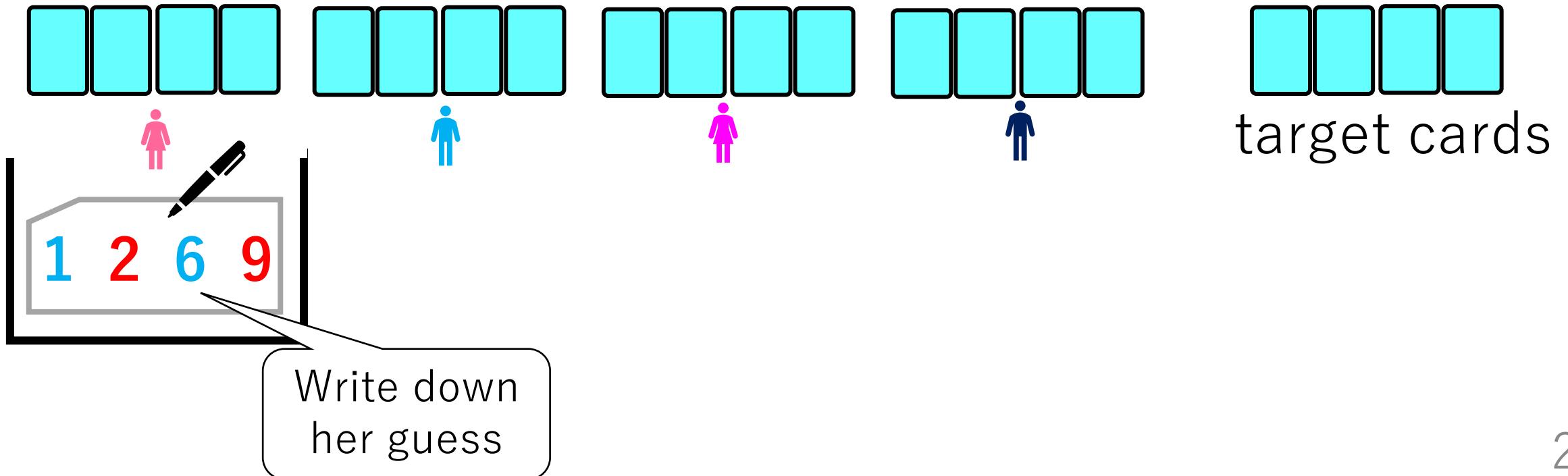
Each player can make a *challenge* anytime, but only once.



target cards

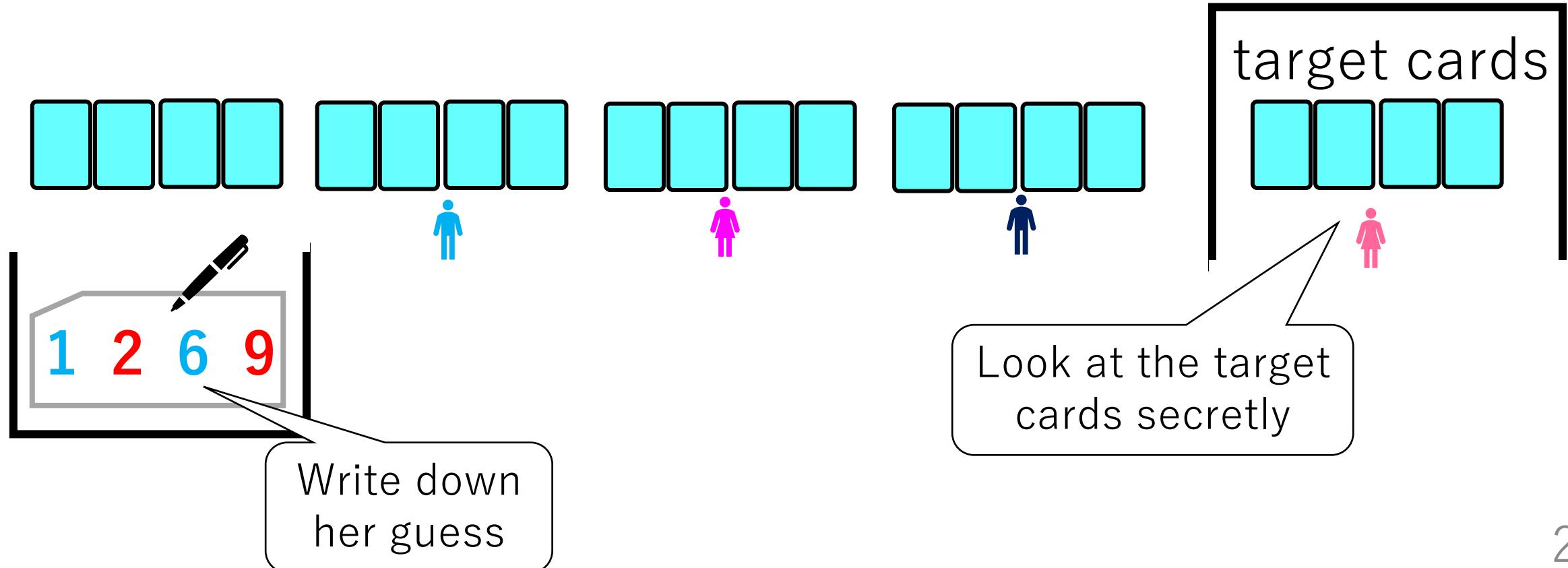
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- The player who challenges writes down their guess.



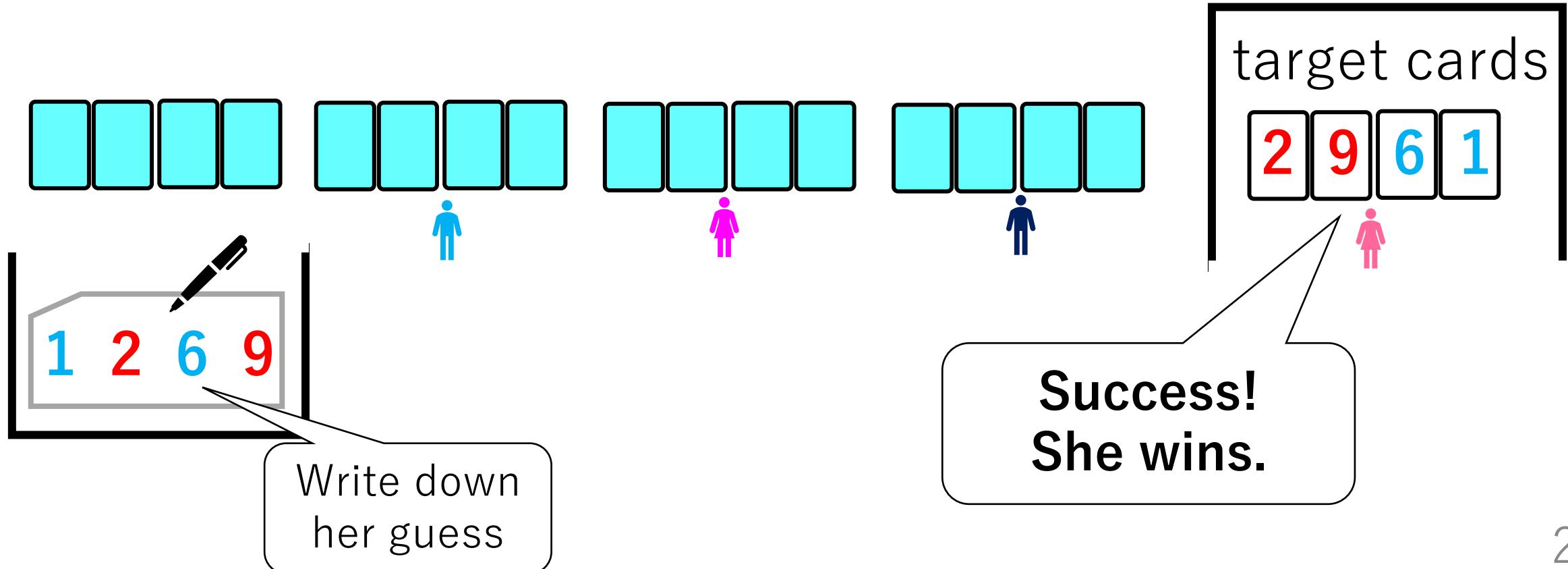
Each player can make a *challenge* anytime, but only once.

- The player who challenges writes down their guess.
- The player **looks at the four face-down target cards** secretly.



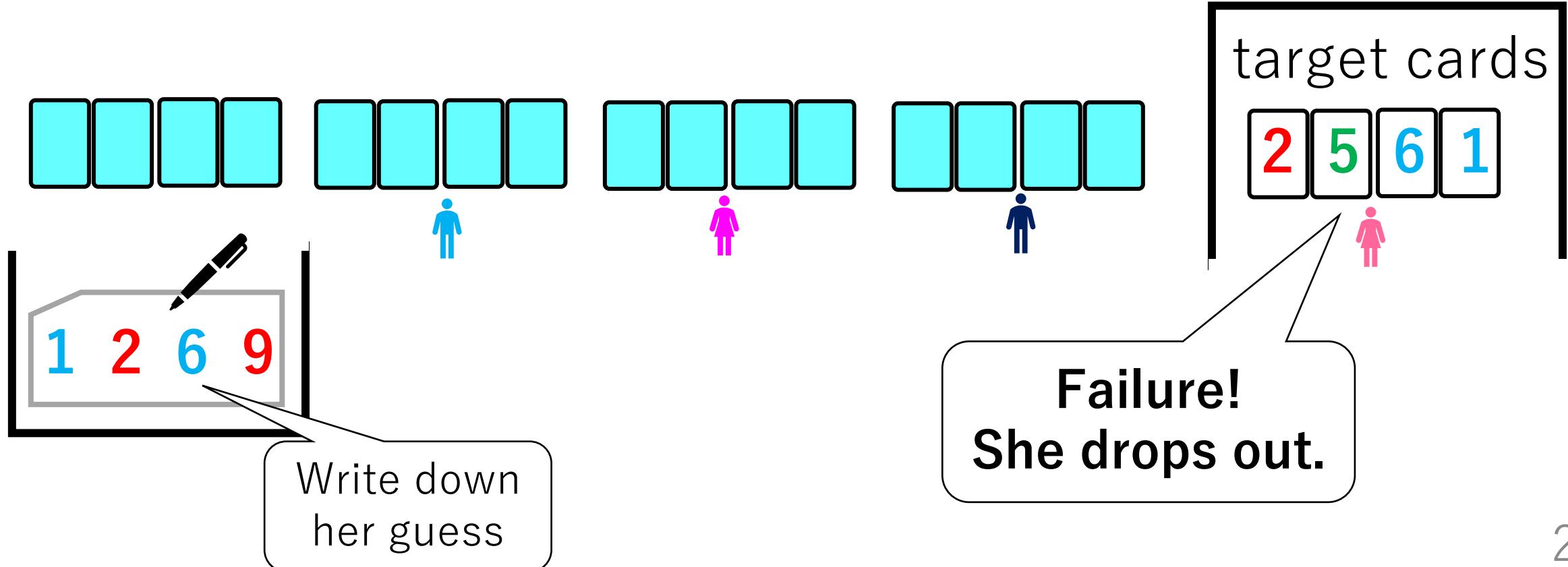
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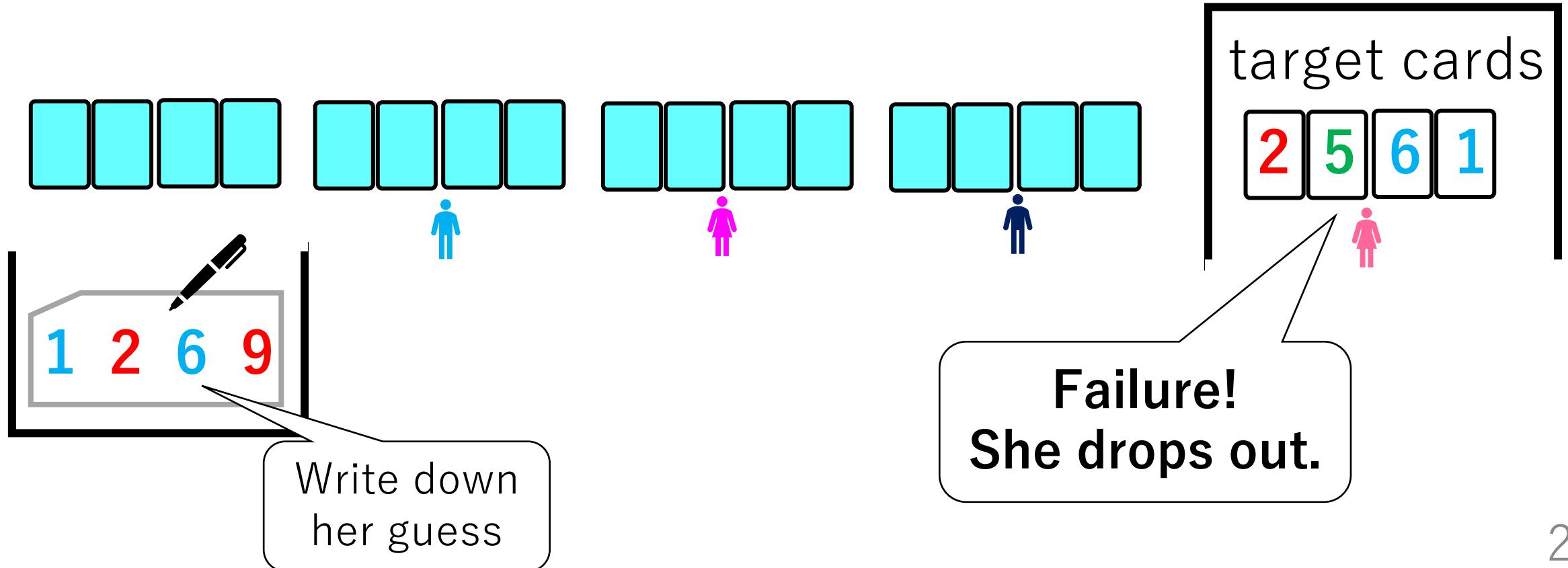


Each player can make a *challenge* anytime, but *only once*.

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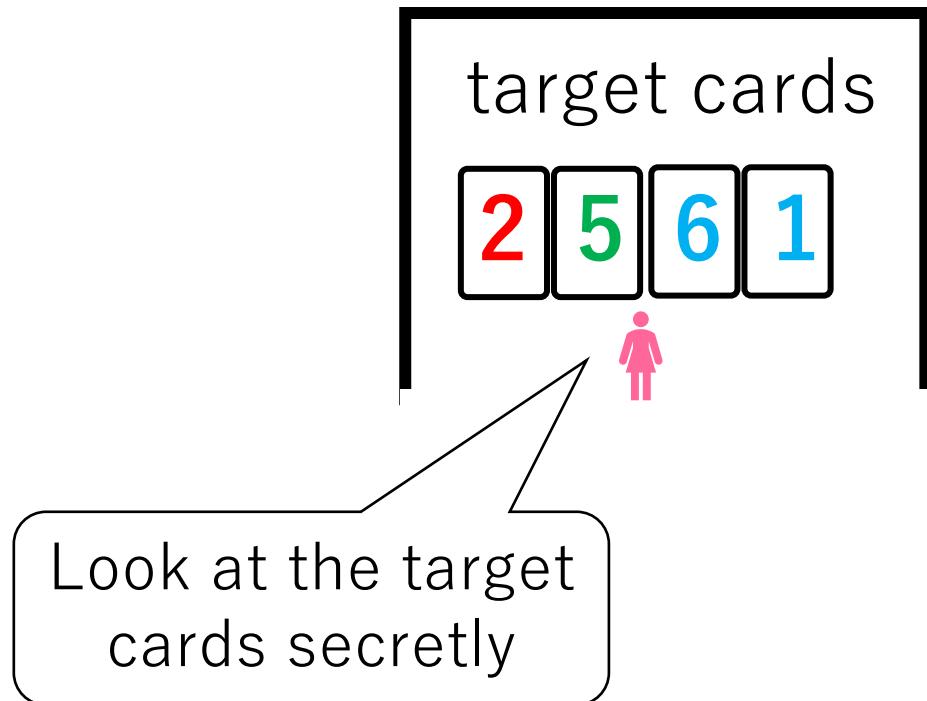


If player's guess is wrong, he or she is eliminated from the game. This is because looking at the target cards makes him/her gain complete knowledge about the target cards.

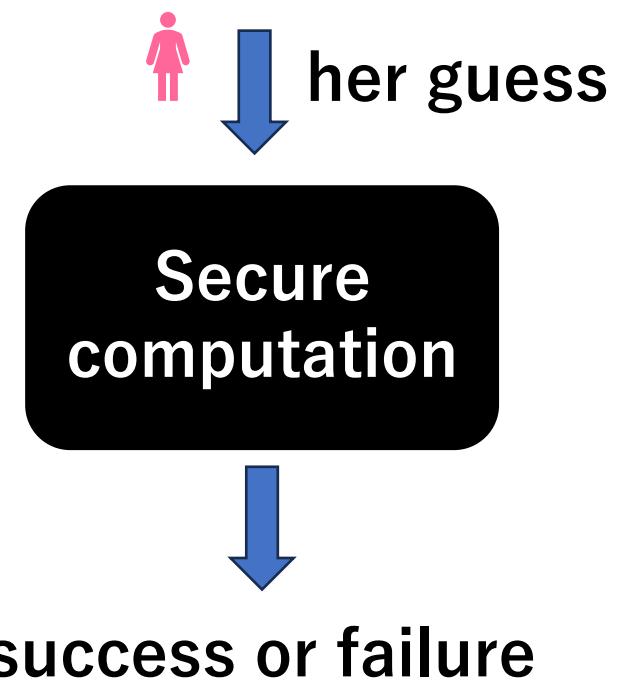


In this study, we explore an *alternative challenge mechanism*.

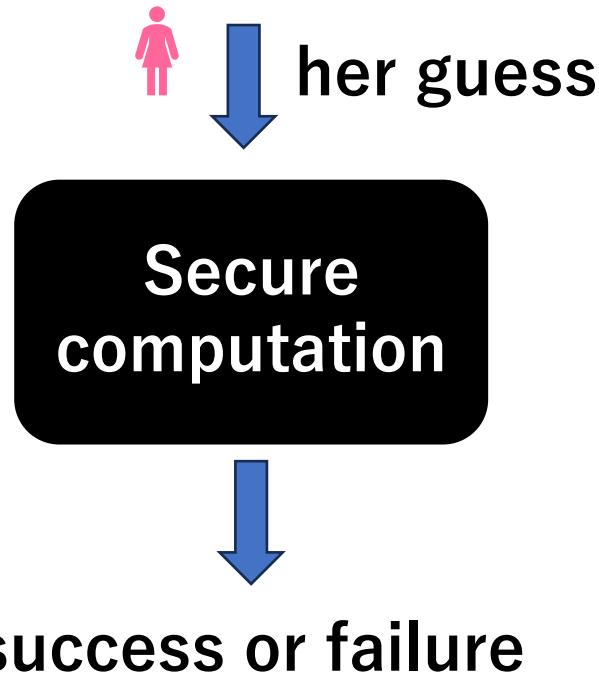
Original



Our method



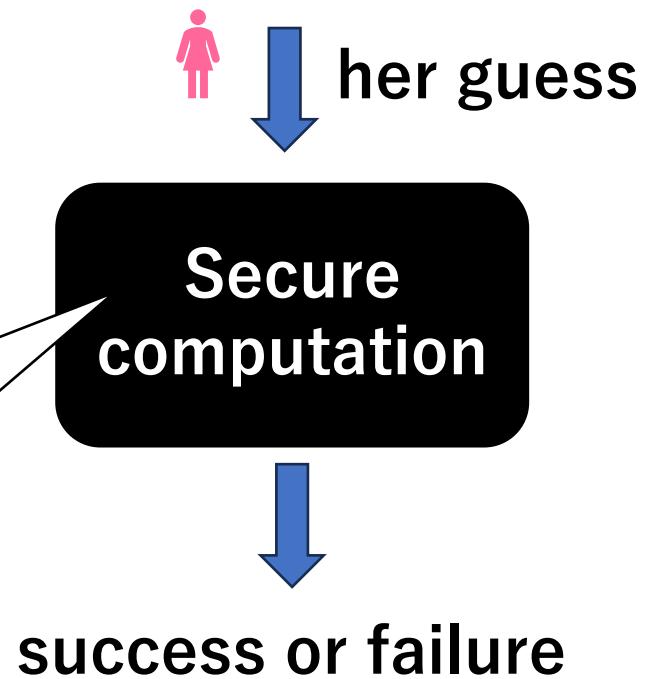
Our method



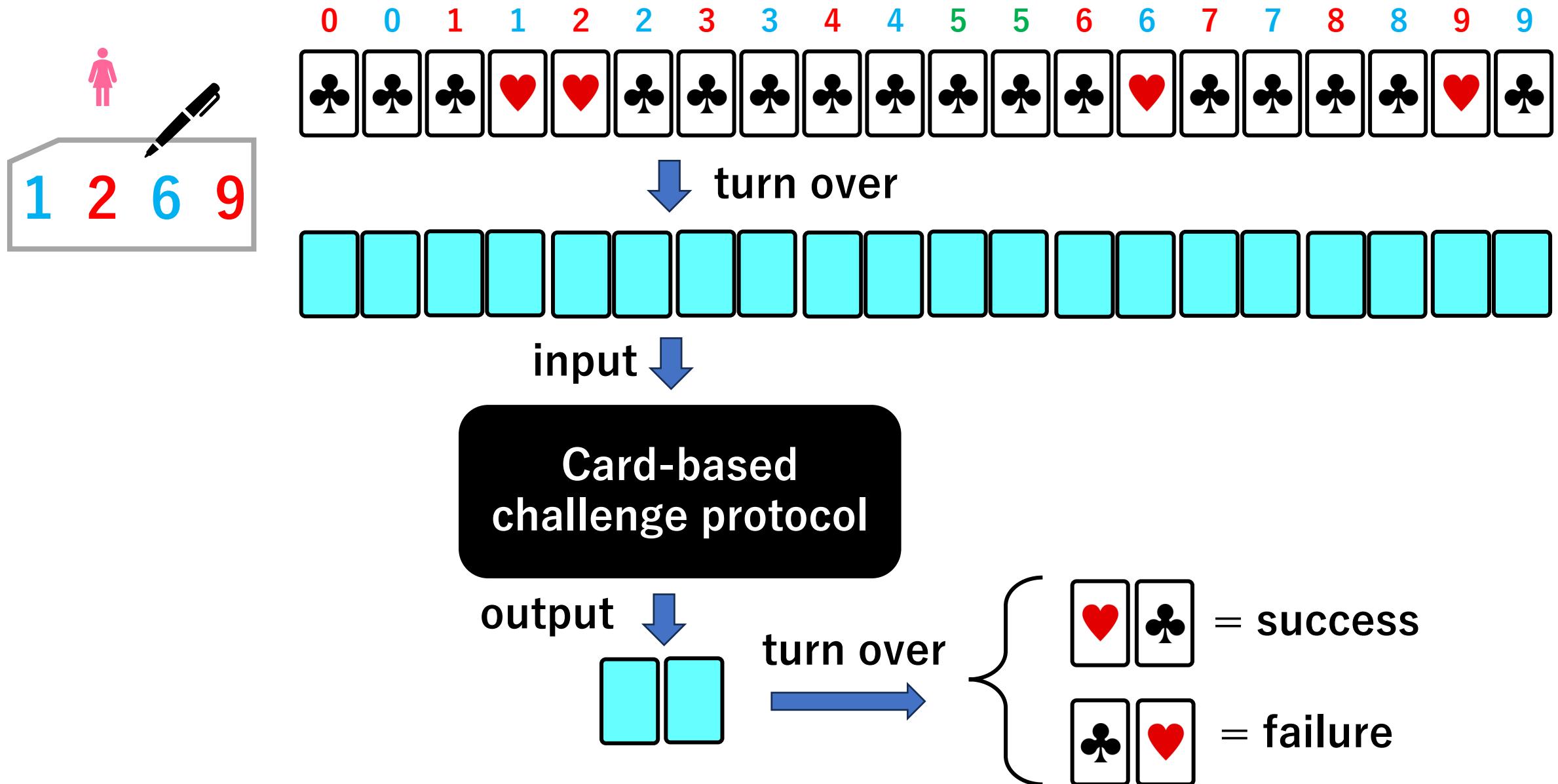
A player who fails a challenge only learns that their guess is incorrect, allowing him/her to continue playing.

Our method

We use card-based cryptography



Our challenge mechanism



Our contribution

By using **card-based cryptography**, we propose a method for securely **determining whether a challenge succeeds or not** without leaking any information (more than necessary).

This provides new game variations of Tagiron; for example, a version could allow players **up to two challenges**, creating new strategic possibilities.

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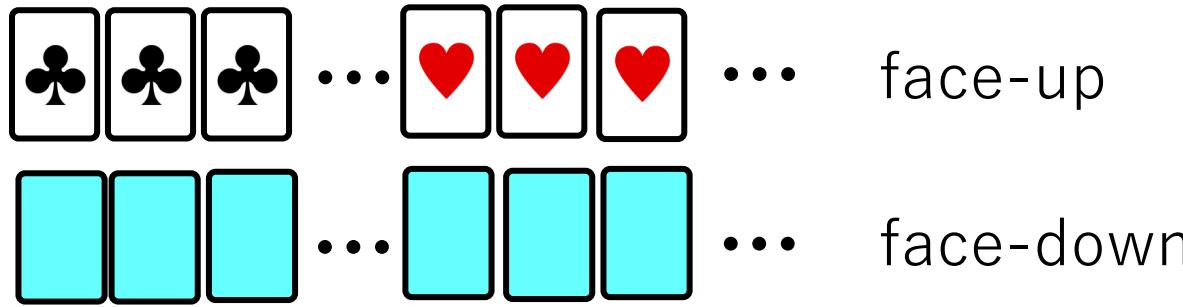
- Card-based cryptography

3. Preprocessing Protocol

4. Challenge Protocol

5. Conclusion

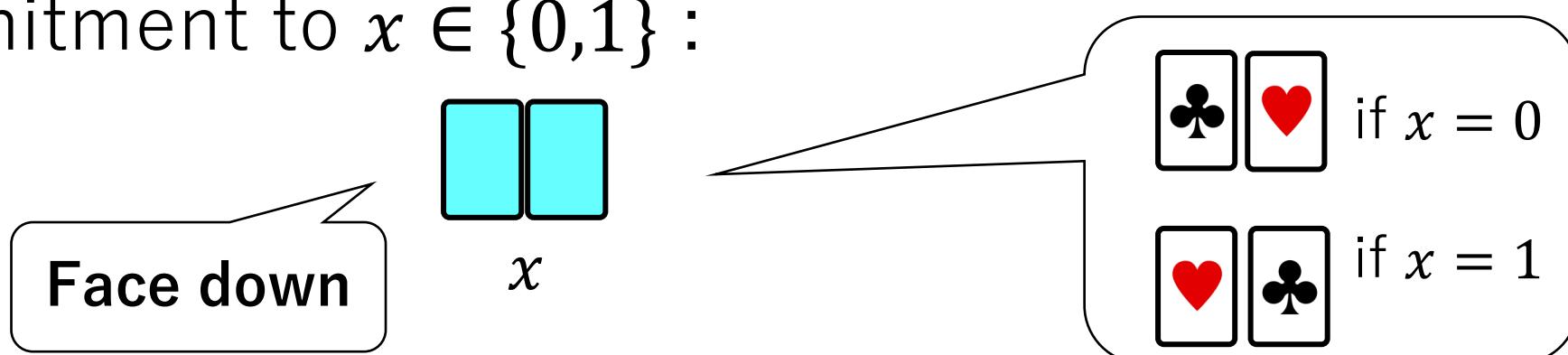
Card-based cryptography



Encoding:

Diagram illustrating the encoding of binary values. Two pairs of cards are shown: a club and a heart, which is labeled $=0$, and a heart and a club, which is labeled $=1$.

Commitment to $x \in \{0,1\}$:



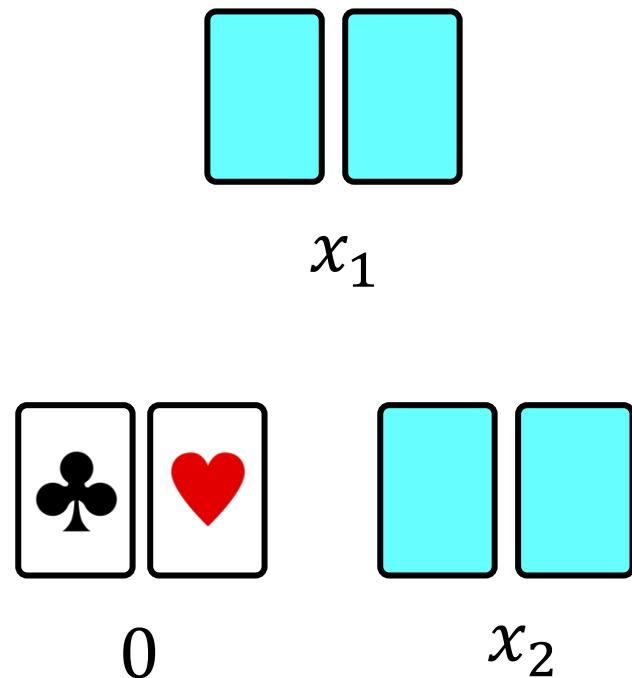
Card-based AND protocol



We want to obtain a commitment to the AND value without leaking any information. How?

AND protocol [MS09]

$$\begin{array}{c} \text{Club} \quad \text{Heart} \\ \text{Heart} \quad \text{Club} \end{array} = 0 \quad \begin{array}{c} \text{Heart} \quad \text{Club} \\ \text{Club} \quad \text{Heart} \end{array} = 1$$

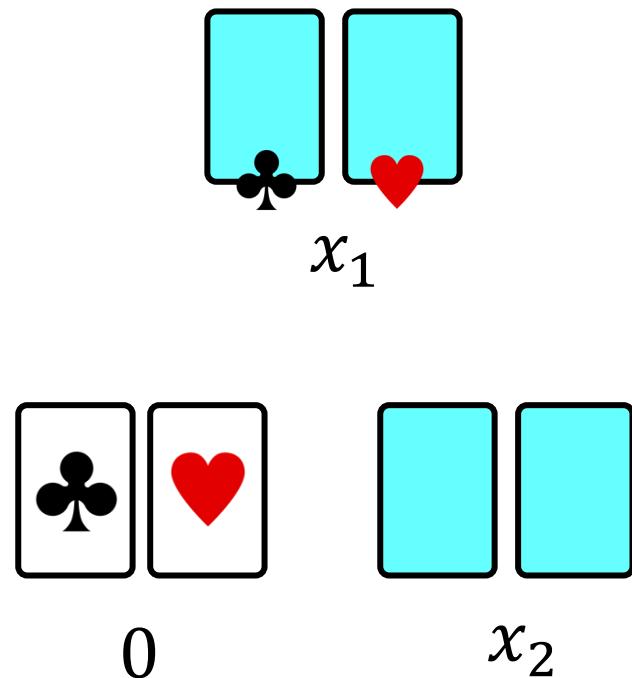


$$x_1 \wedge x_2 = \begin{cases} 0, & x_1 = 0 \\ x_2, & x_1 = 1 \end{cases}$$

[MS09] Takaaki Mizuki and Hideaki Sone. Six-card secure AND and four-card secure XOR, Frontiers in Algorithmics, volume 5598 of LNCS, pages 358–369, Berlin, Heidelberg, 2009. Springer.

AND protocol [MS09]

$$\begin{array}{c} \text{Club} \quad \text{Heart} \\ \text{Club} \quad \text{Heart} \end{array} = 0 \quad \begin{array}{c} \text{Heart} \quad \text{Club} \\ \text{Heart} \quad \text{Club} \end{array} = 1$$

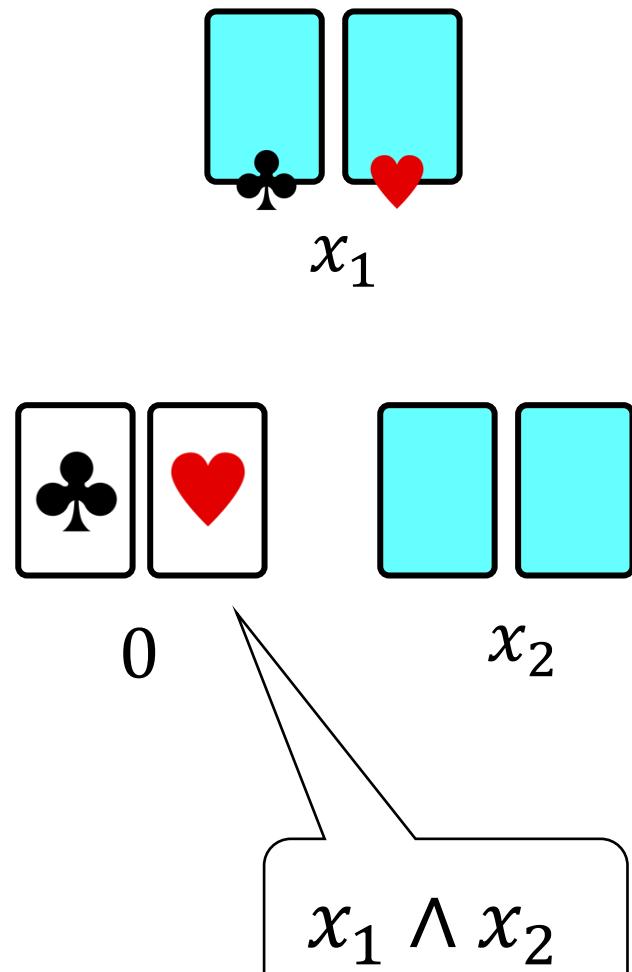


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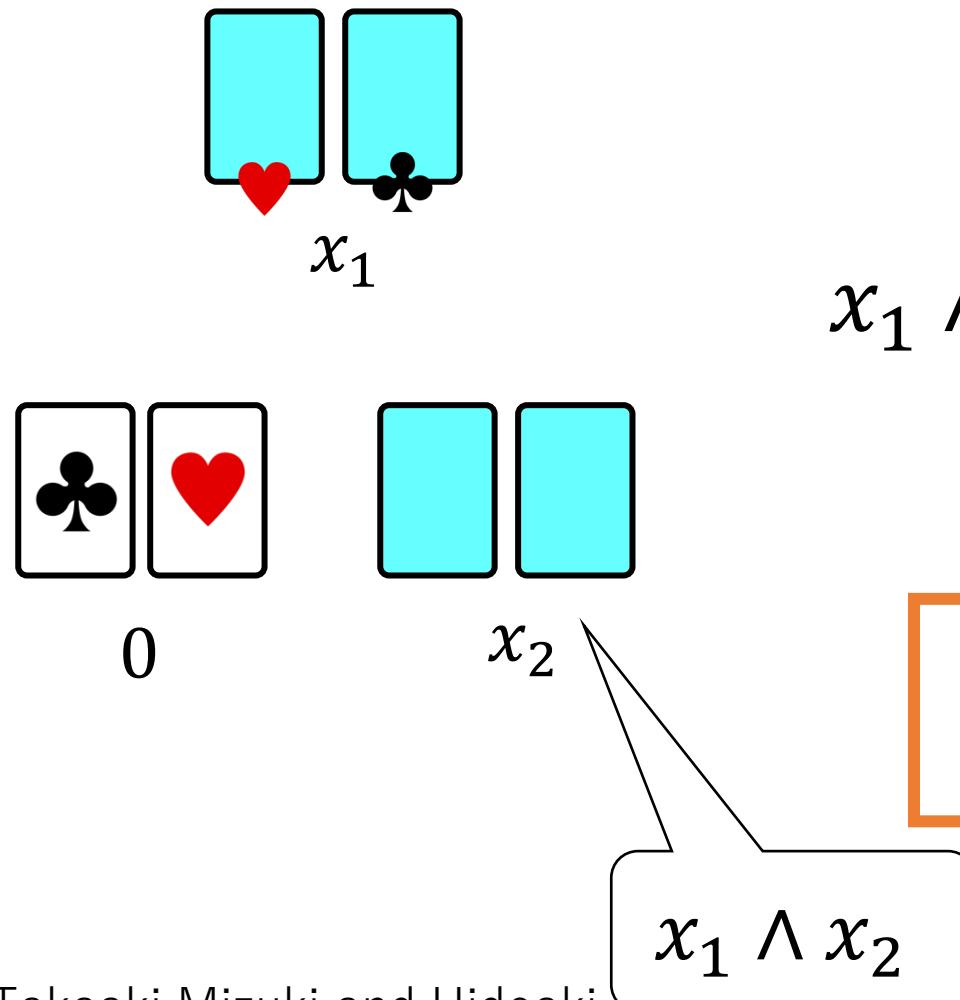


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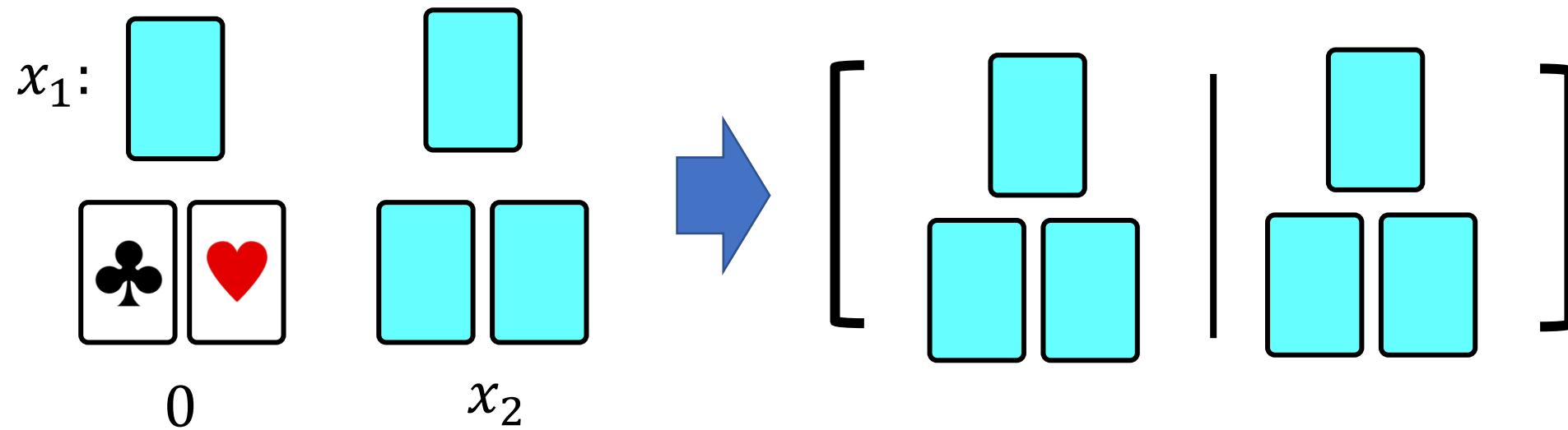
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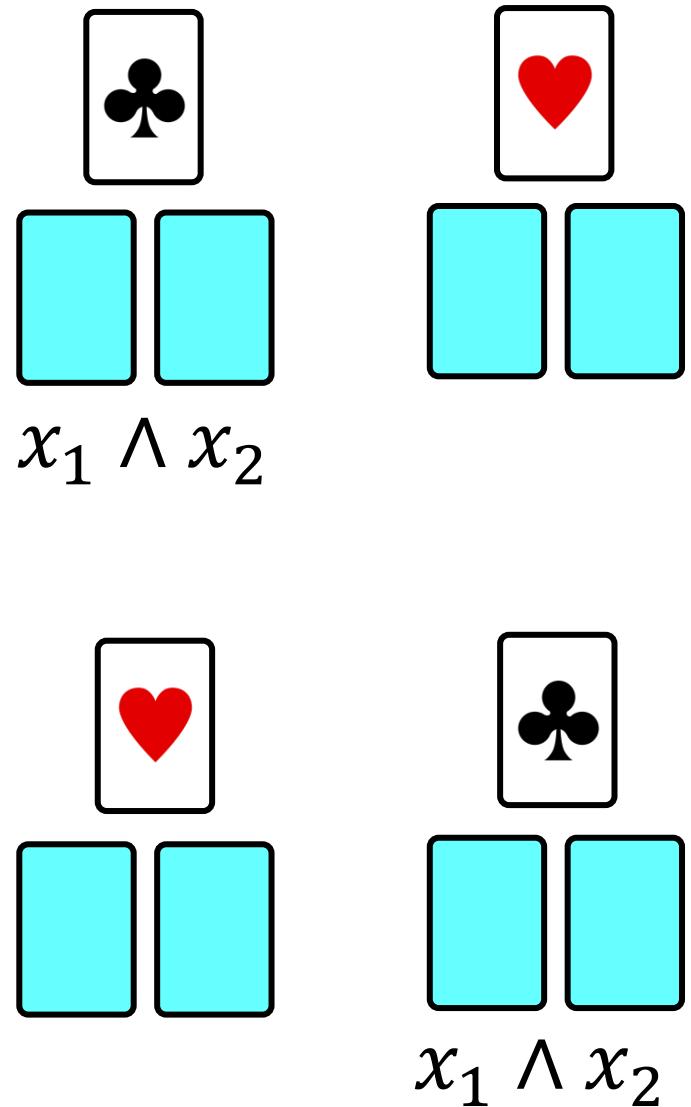
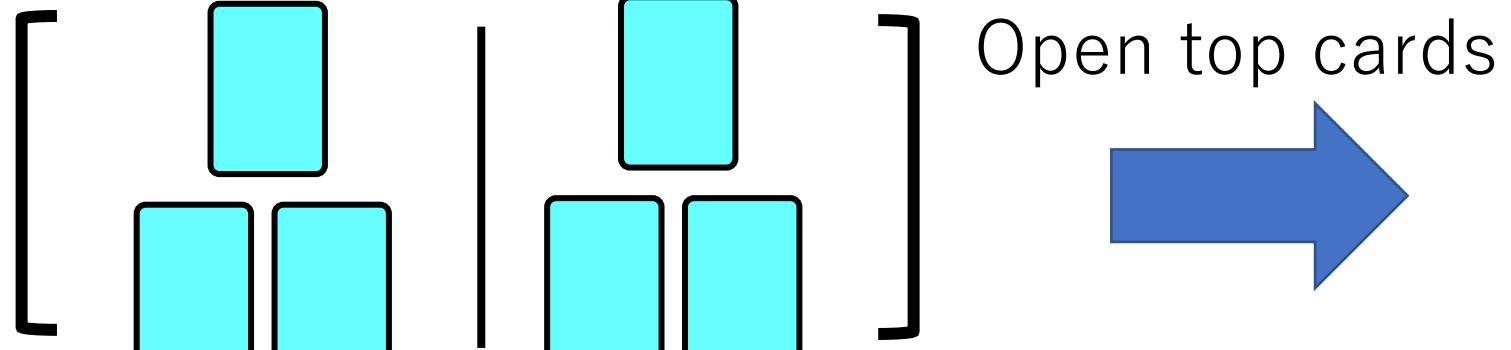
AND protocol [MS09]

$$\begin{array}{c} \text{Club} \quad \text{Heart} \\ \text{Card 1} \quad \text{Card 2} \end{array} = 0 \quad \begin{array}{c} \text{Heart} \quad \text{Club} \\ \text{Card 1} \quad \text{Card 2} \end{array} = 1$$



Shuffle the two portions

AND protocol [MS09]



[MS09] Takaaki Mizuki and Hideaki Sone. Six-card secure AND and four-card secure XOR, Frontiers in Algorithmics, volume 5598 of LNCS, pages 358–369, Berlin, Heidelberg, 2009. Springer.

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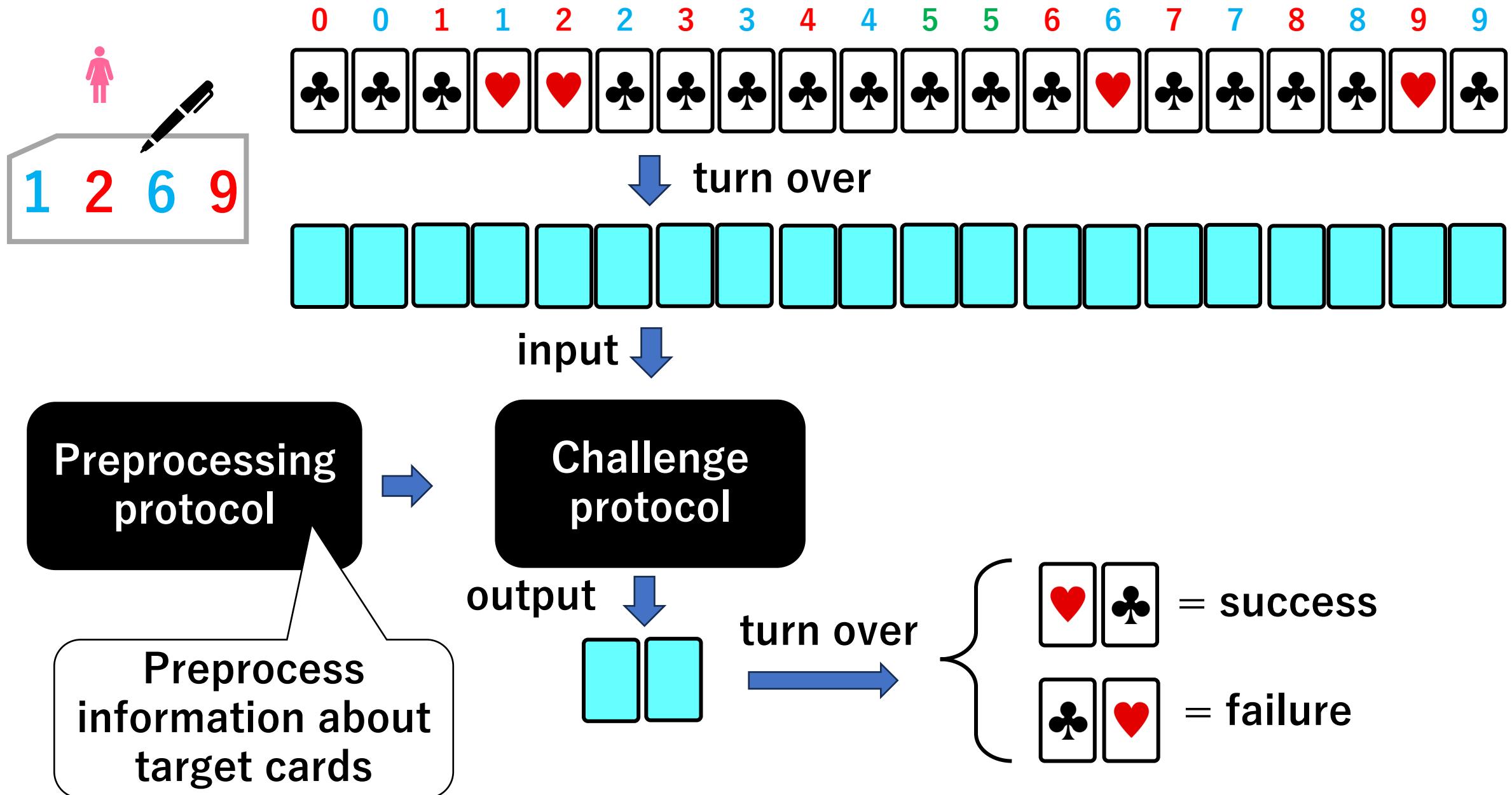
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Our method



Tagiron cards



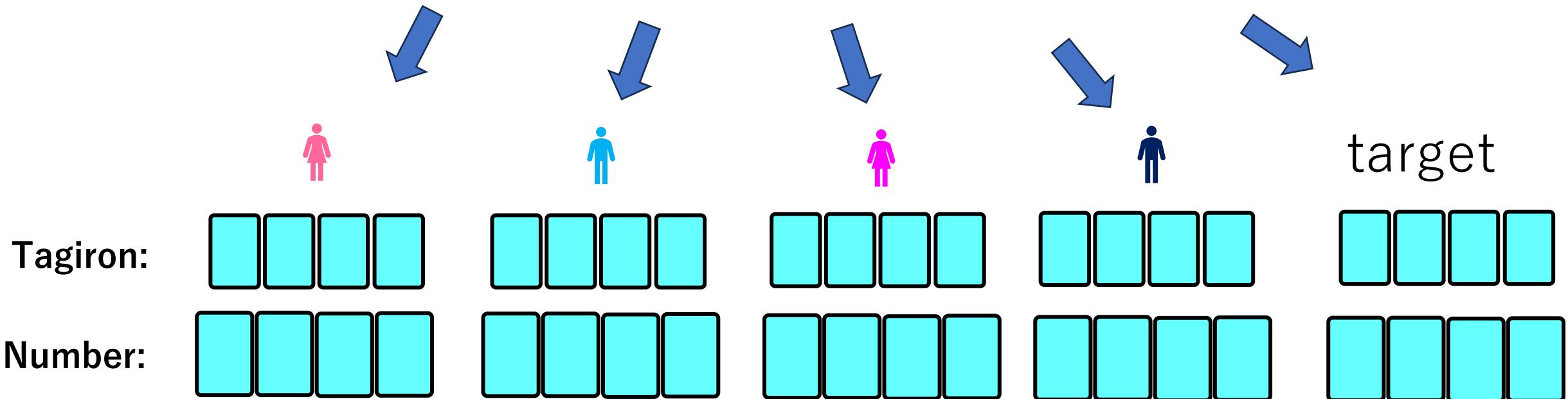
Number cards



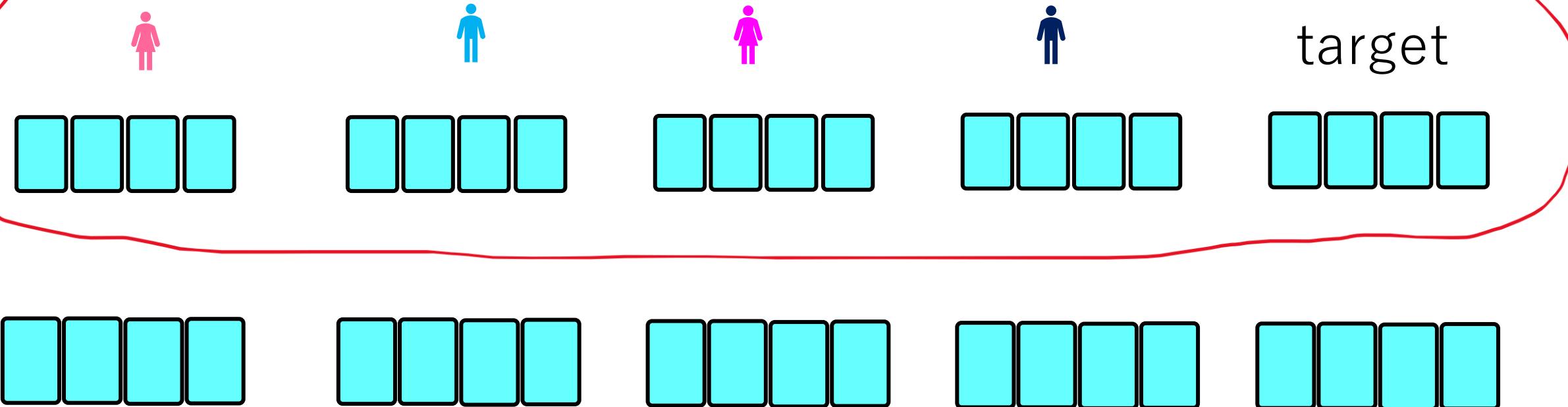
Correspondence

| | | | | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|
| 0 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 | 6 | 6 | 7 | 7 | 8 | 8 | 9 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |

Tagiron cards along with number cards are distributed:



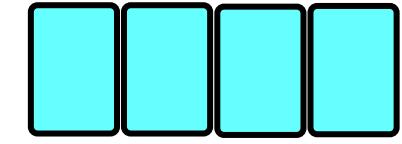
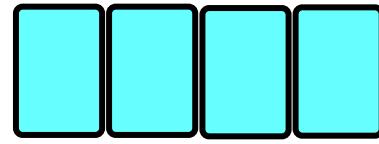
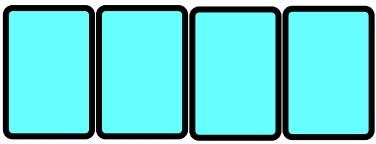
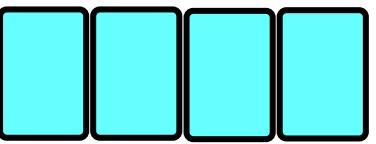
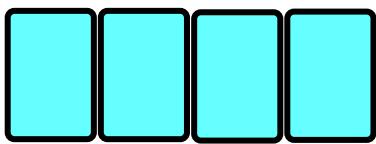
Tagiron cards are used as in a normal game:



Number cards are used in the preprocessing protocol and challenge protocol

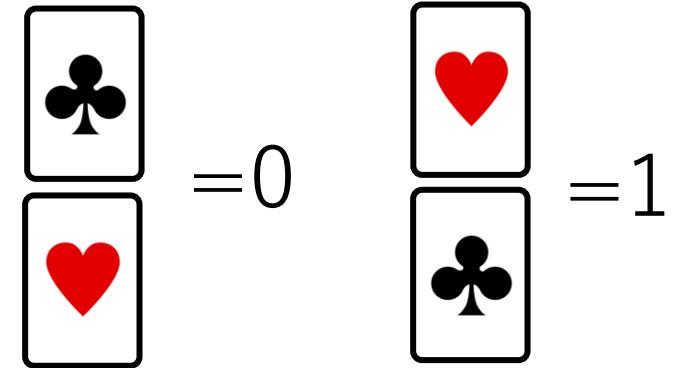
Preprocessing protocol

Number
cards

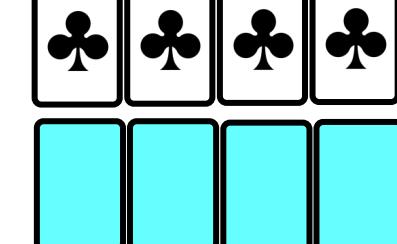
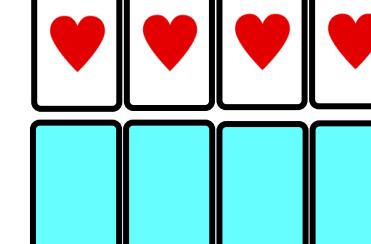
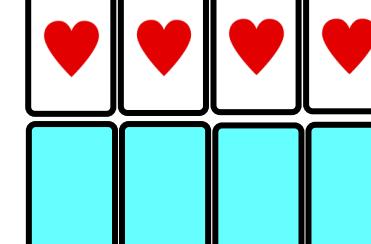
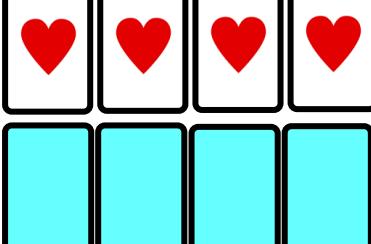
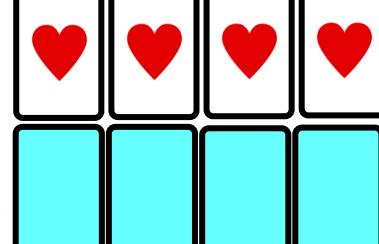
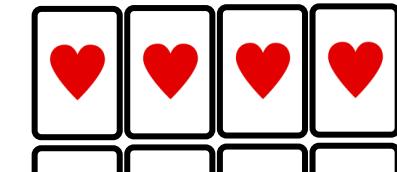
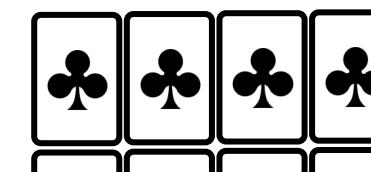
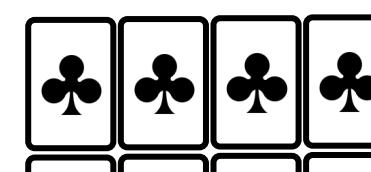
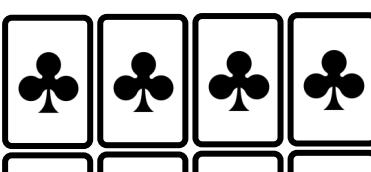
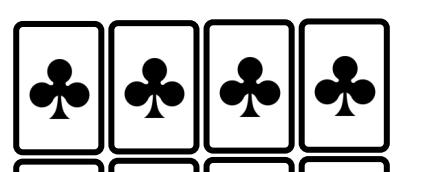


target

Preprocessing protocol



Place 0 above players' cards, and 1 above the target cards:

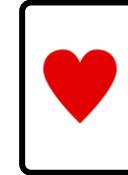
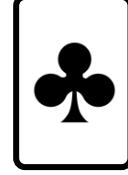
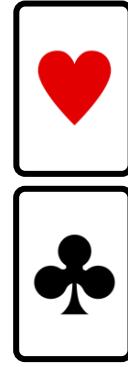


Number
cards

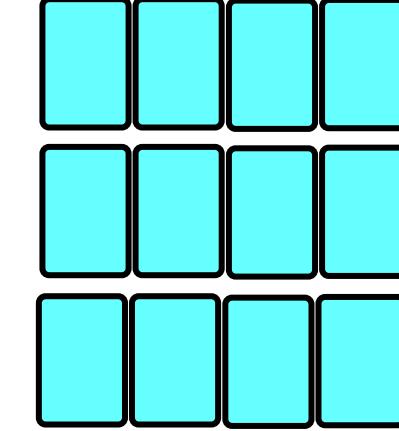
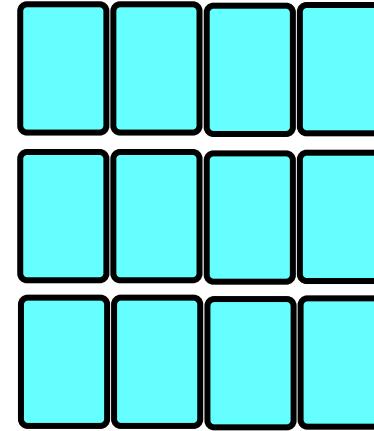
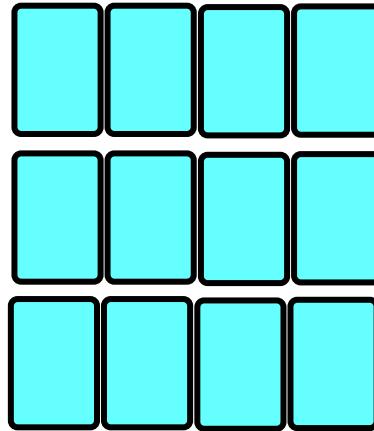
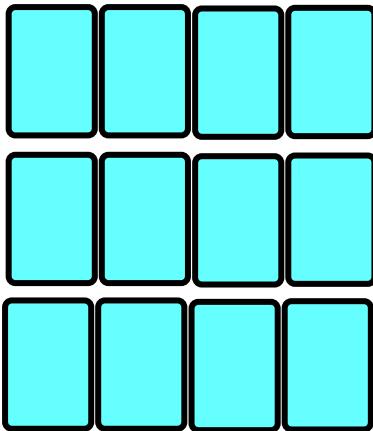
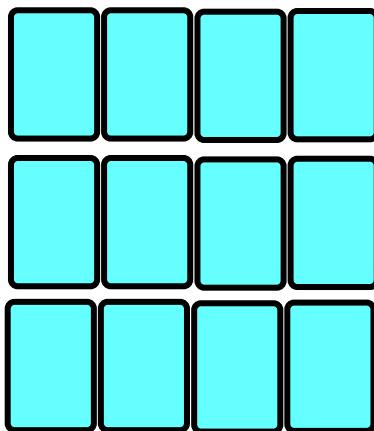


target

Preprocessing protocol

 $=0$  $=1$ 

Turn over all face-up cards:

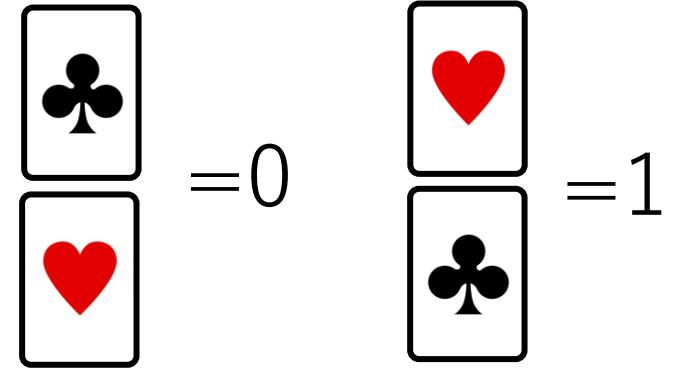


Number
cards

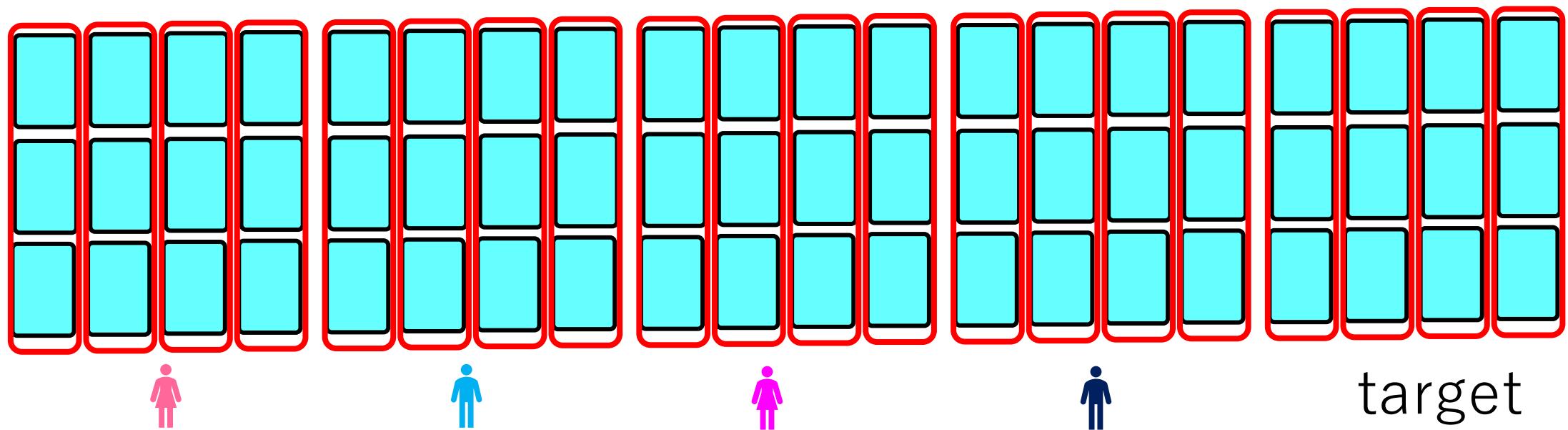


target

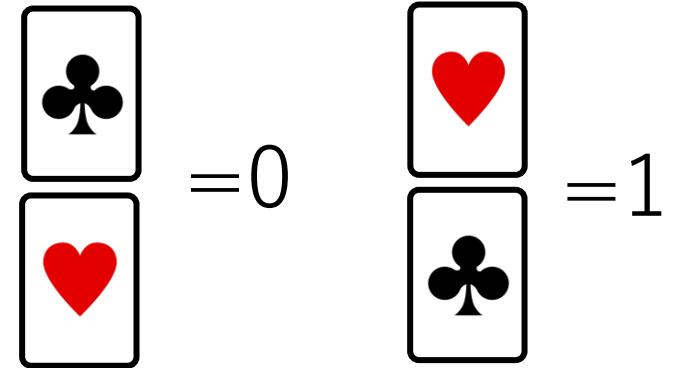
Preprocessing protocol



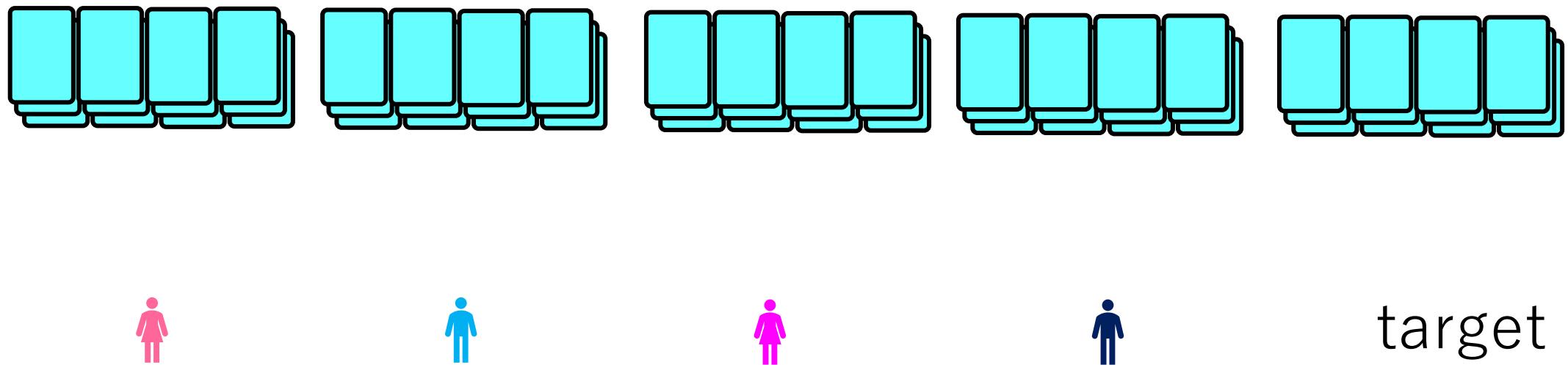
Make 3-card piles:



Preprocessing protocol

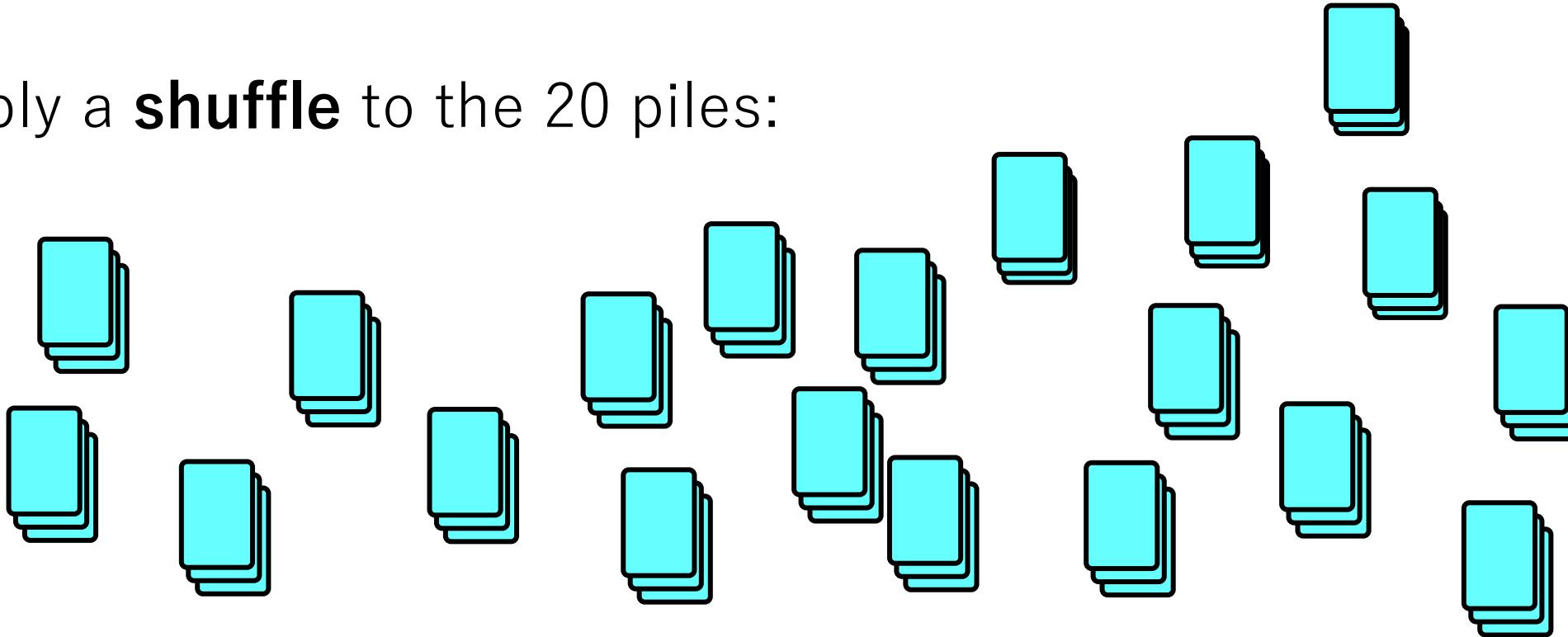


Make 3-card piles:



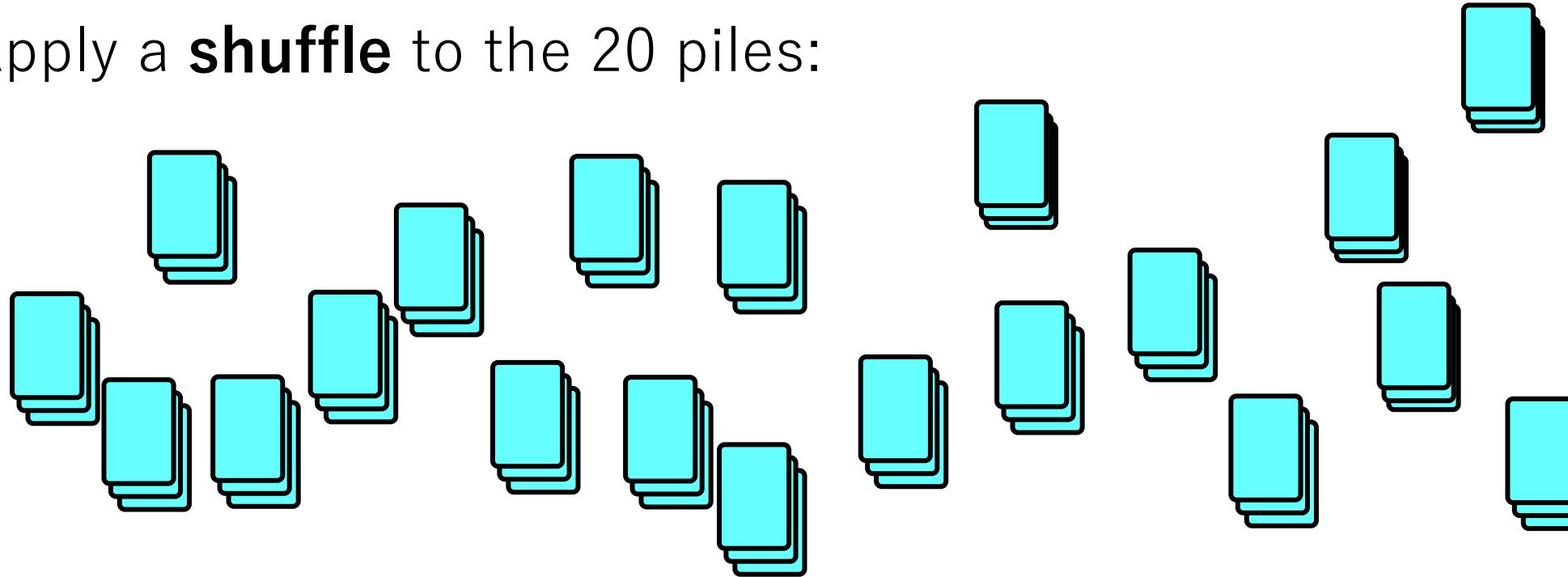
Preprocessing protocol

Apply a **shuffle** to the 20 piles:



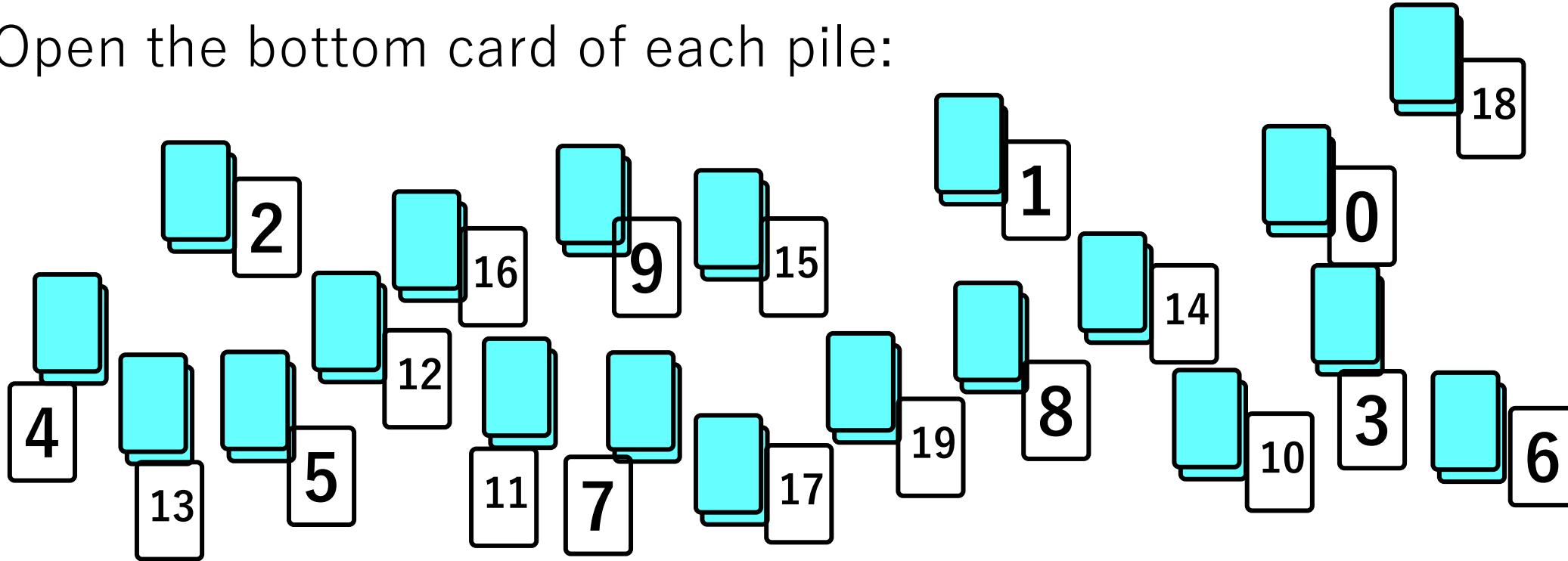
Preprocessing protocol

Apply a **shuffle** to the 20 piles:



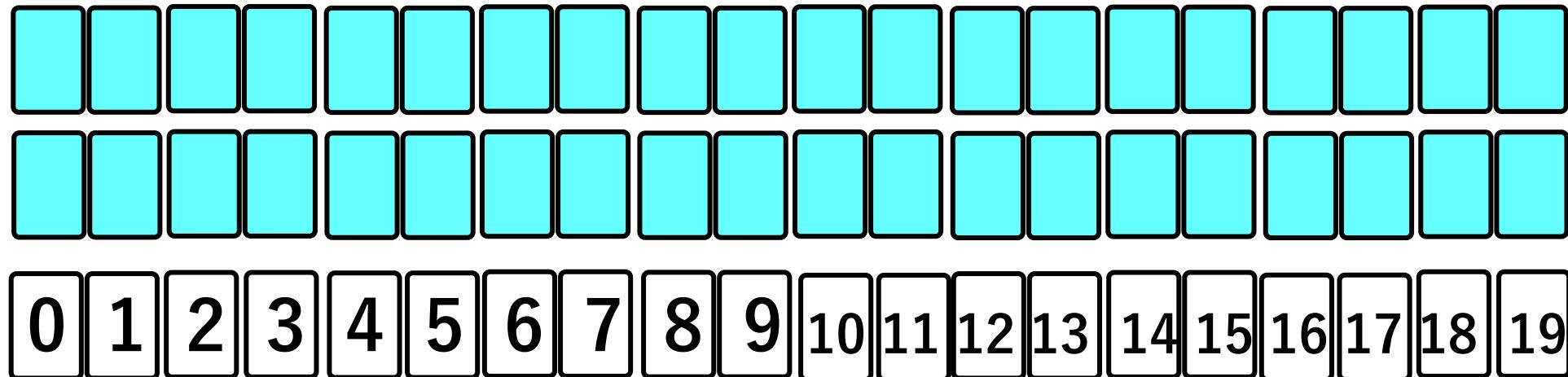
Preprocessing protocol

Open the bottom card of each pile:

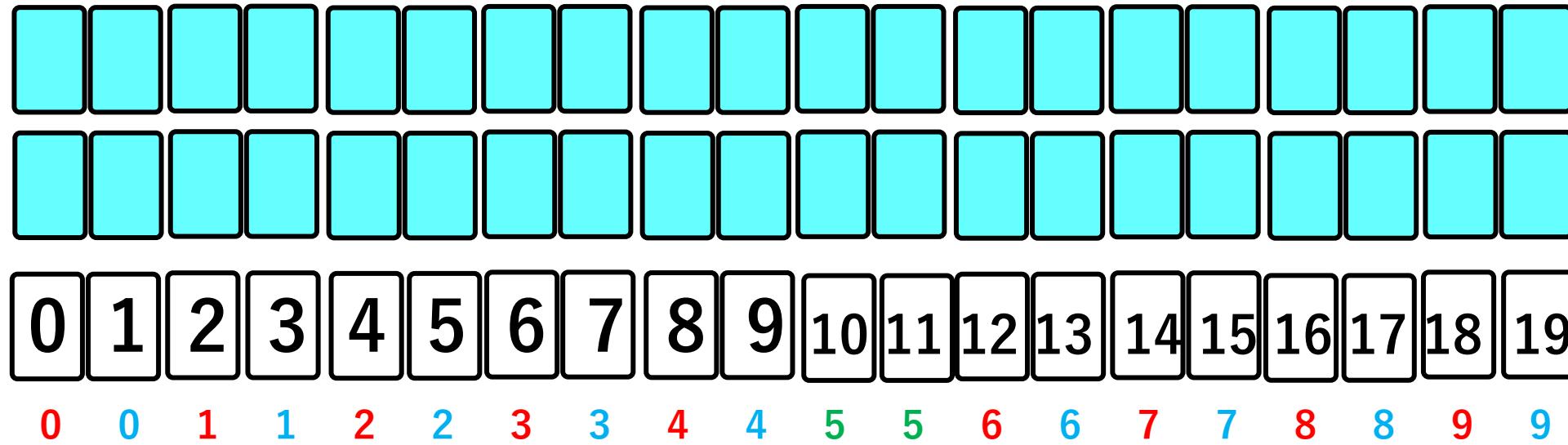


Preprocessing protocol

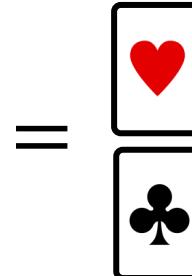
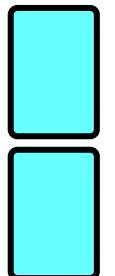
Sort the piles based on the bottom cards:



Preprocessing protocol



target card

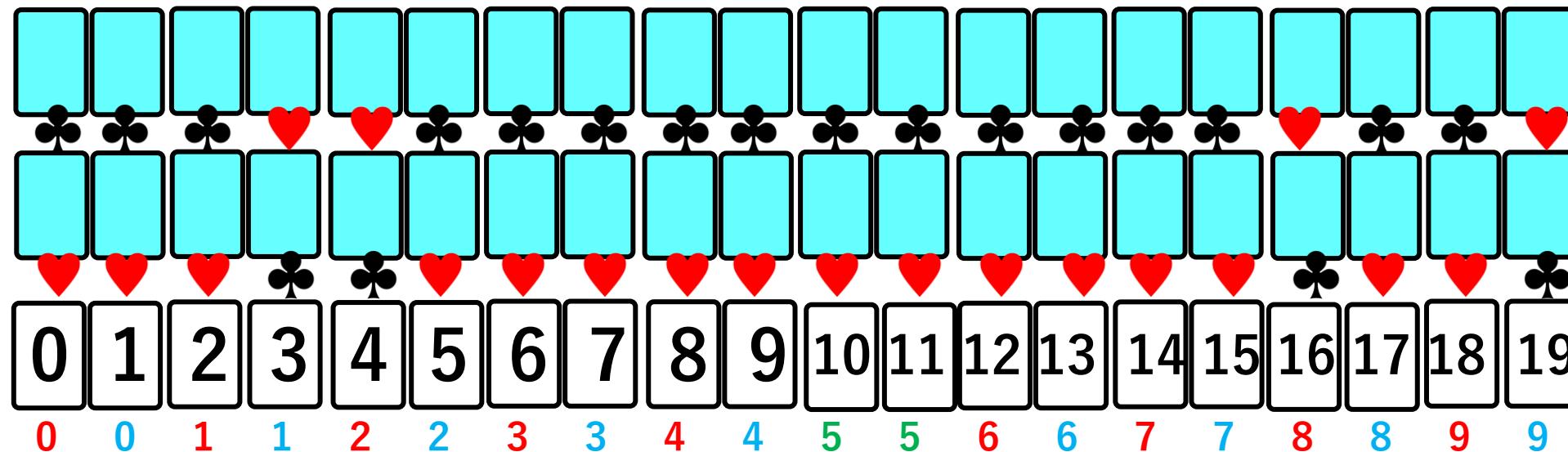


= 1

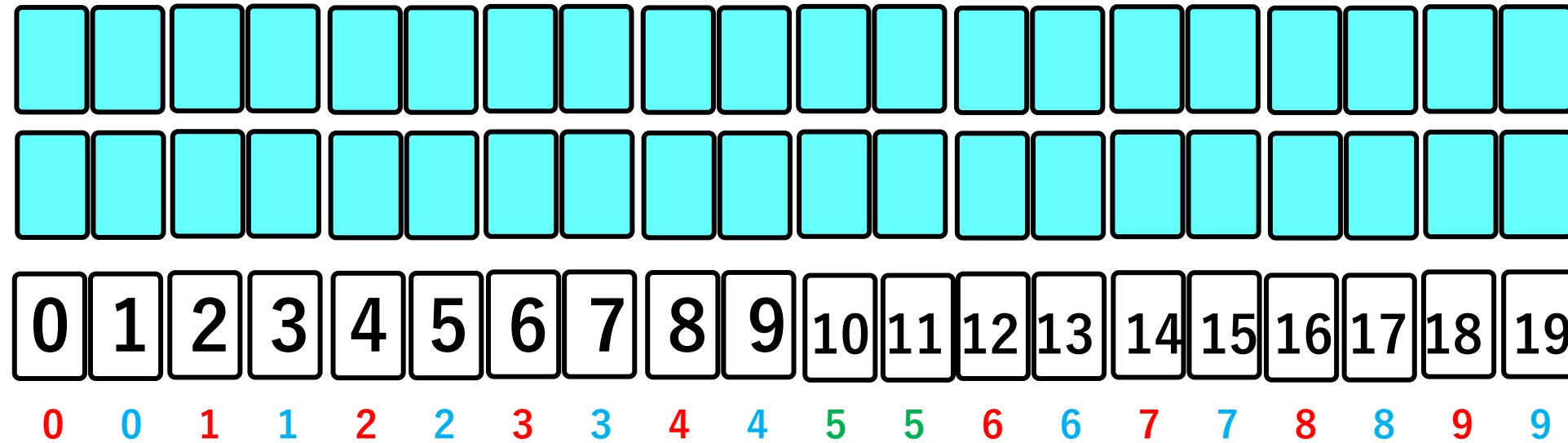
For example, if target cards are

2 1 9 8

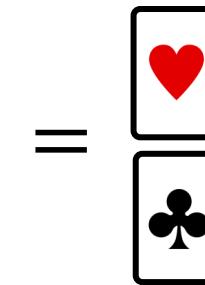
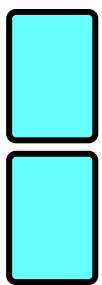
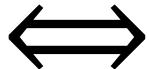
 = 0  = 1



Preprocessing protocol



target card



= 1

This is the preprocessing protocol.

(Here, we omit the steps for handling two green cards)

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1. Introduction

- Tagiron's rules
- Our contribution

2. Preliminaries

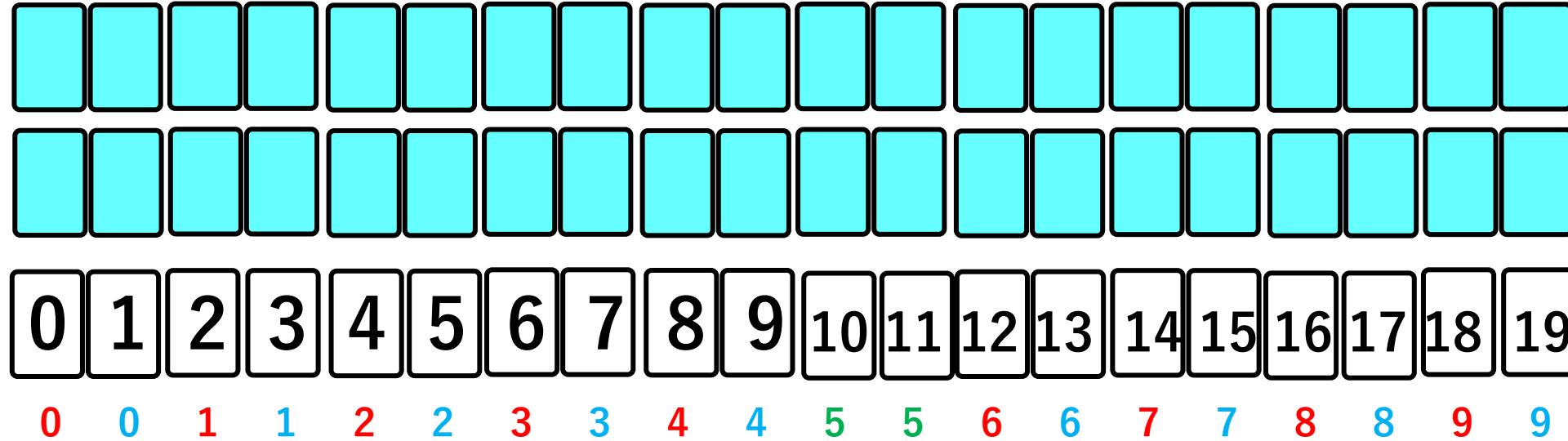
- Card-based cryptography

3. Preprocessing Protocol

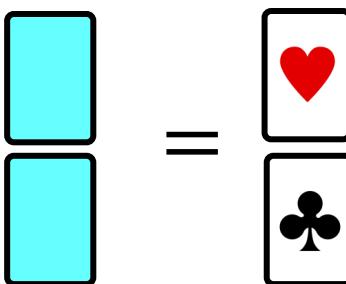
4. Challenge Protocol

5. Conclusion

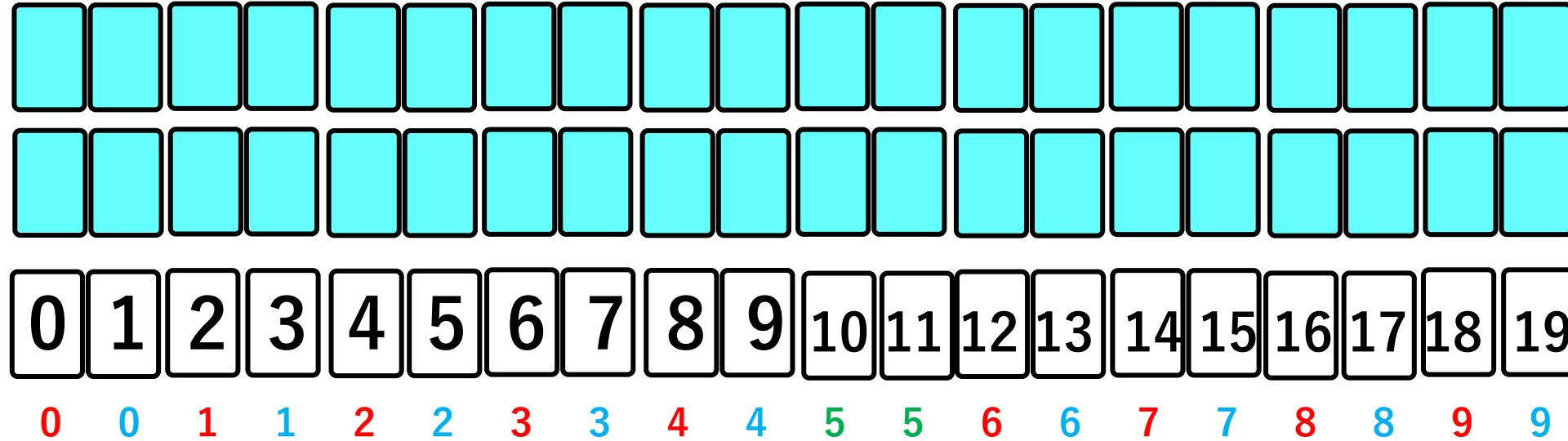
By the preprocessing protocol, we have:



target card \iff



A player wants to make a challenge:

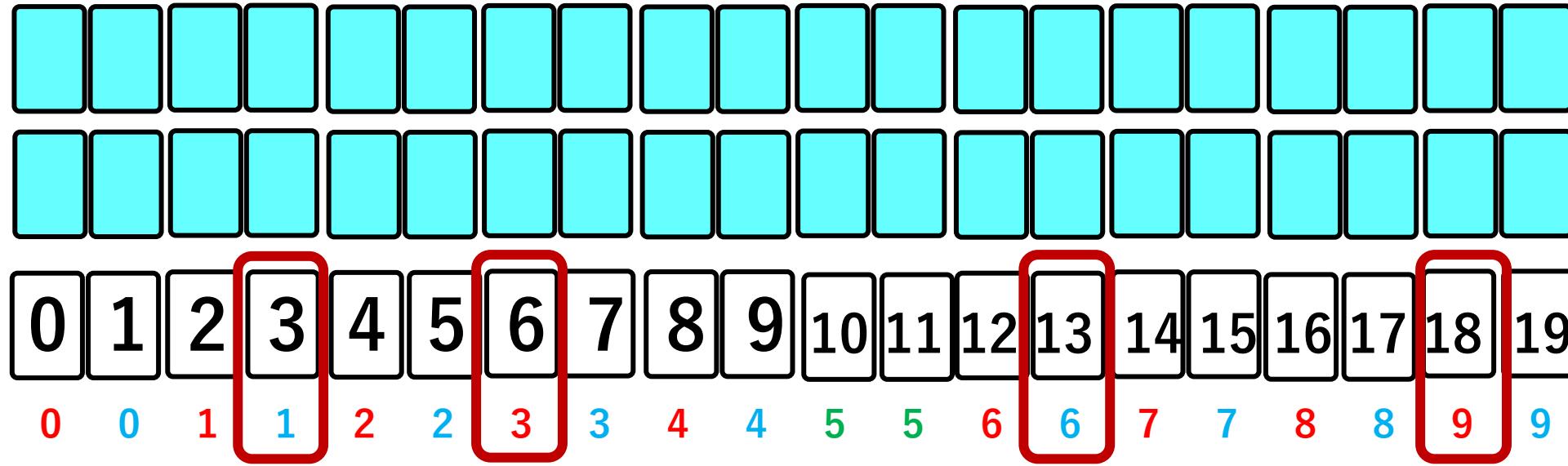


My guess is

1 3 6 9



A player wants to make a challenge:

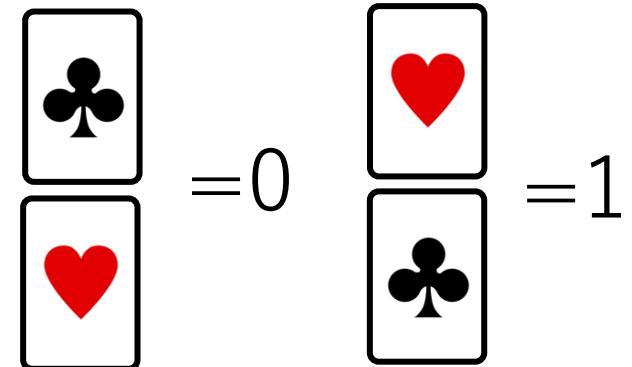
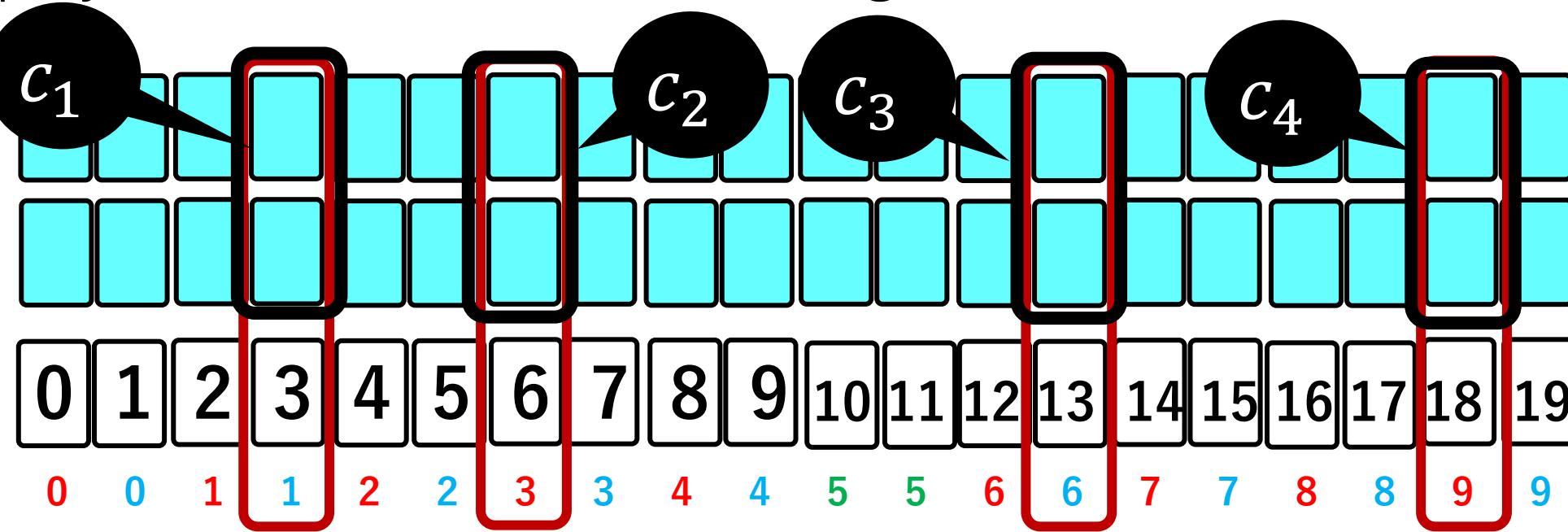


My guess is

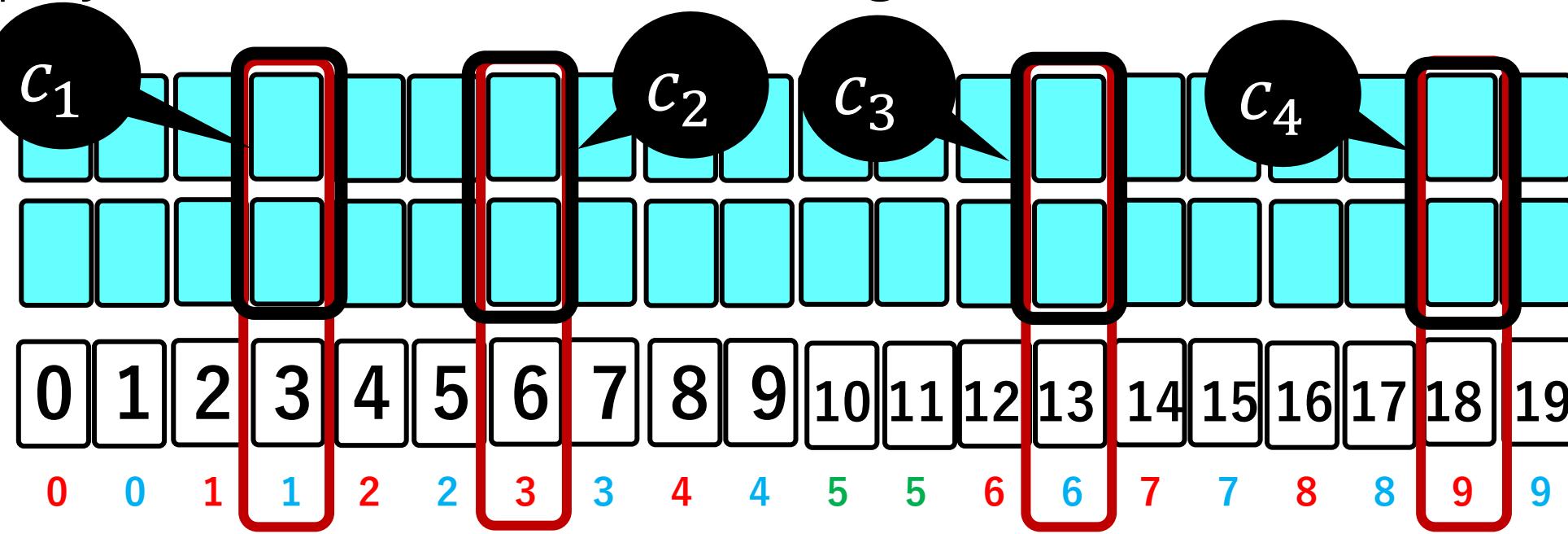
1 3 6 9



A player wants to make a challenge:



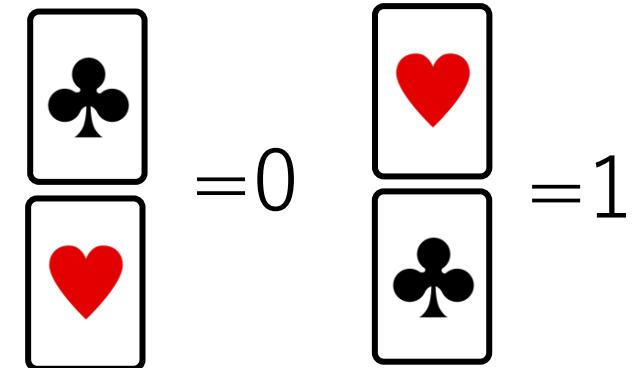
A player wants to make a challenge:



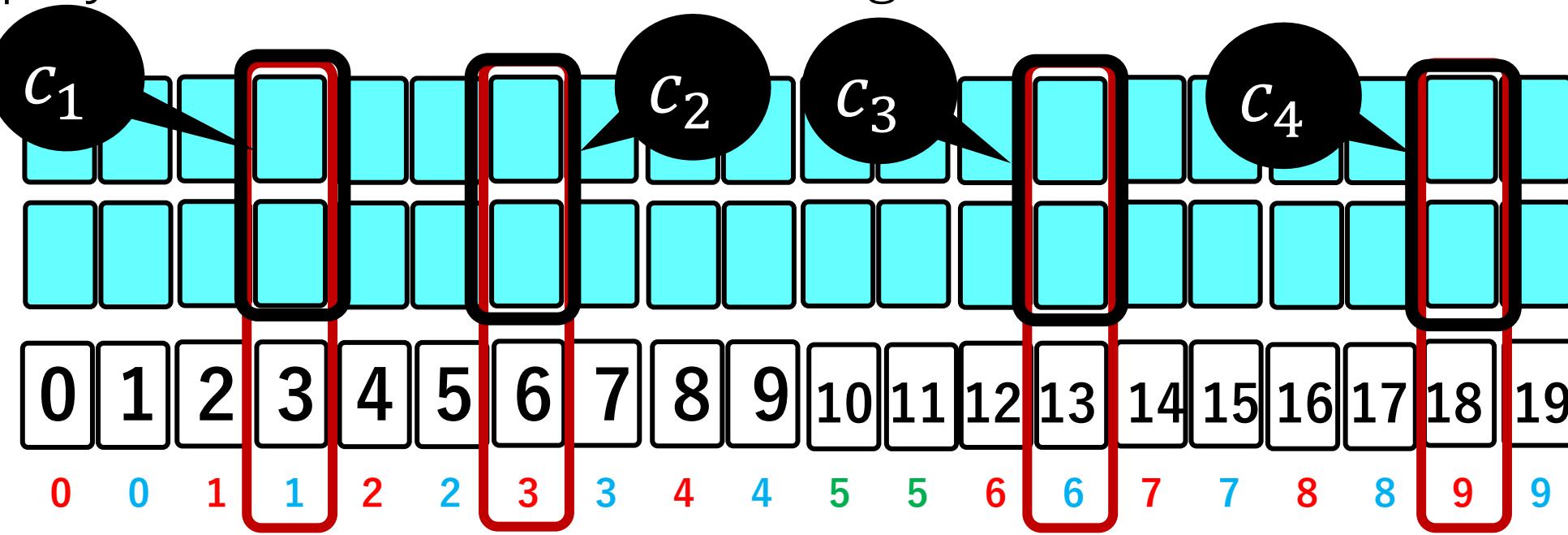
guess is correct



$$c_1 = c_2 = c_3 = c_4 = 1$$



A player wants to make a challenge:



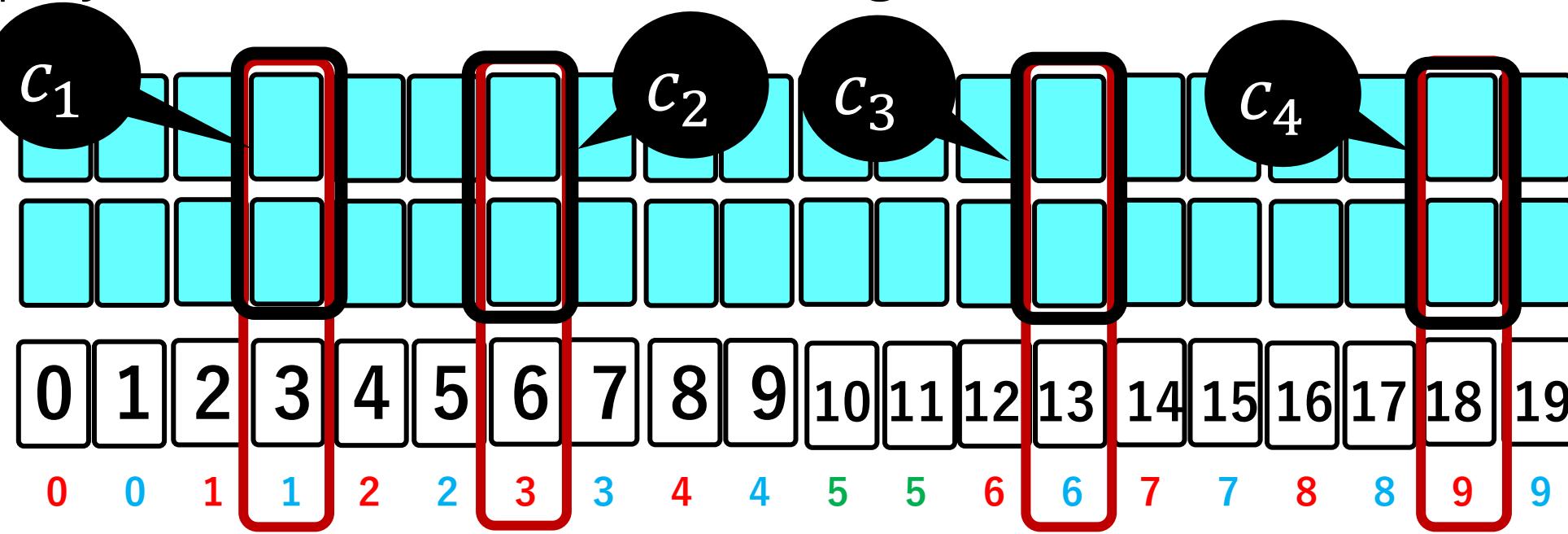
My guess is
1 3 6 9



$c_1 \wedge c_2 \wedge c_3 \wedge c_4 = 1 \rightarrow \text{success}$

$c_1 \wedge c_2 \wedge c_3 \wedge c_4 = 0 \rightarrow \text{failure}$

A player wants to make a challenge:



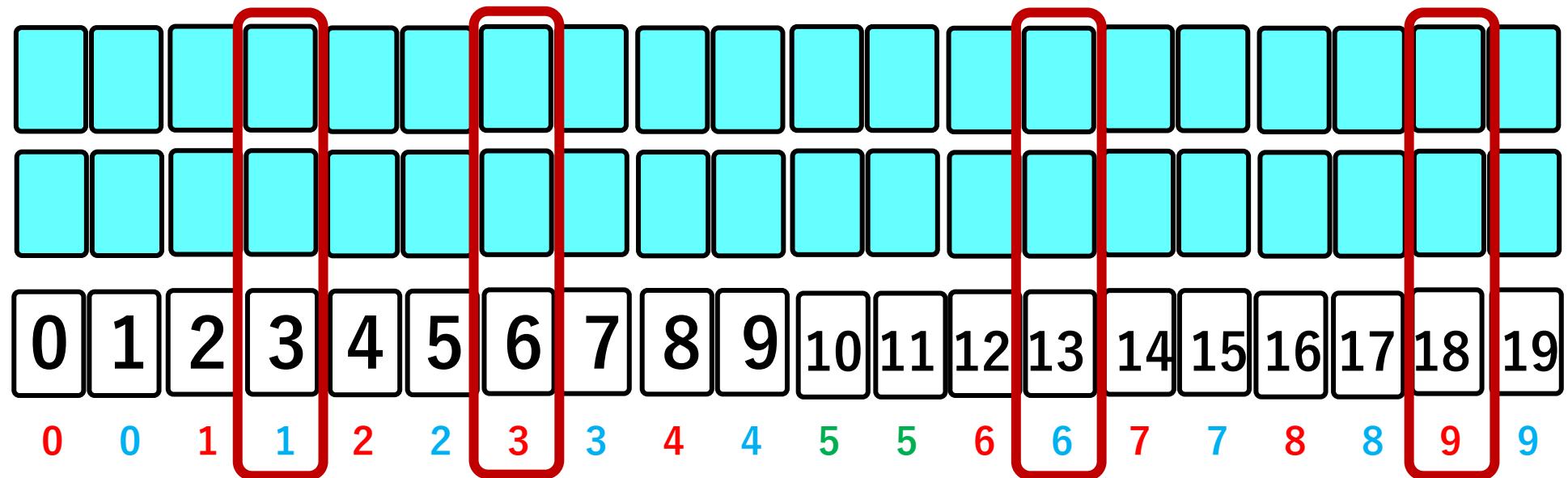
My guess is

1 3 6 9

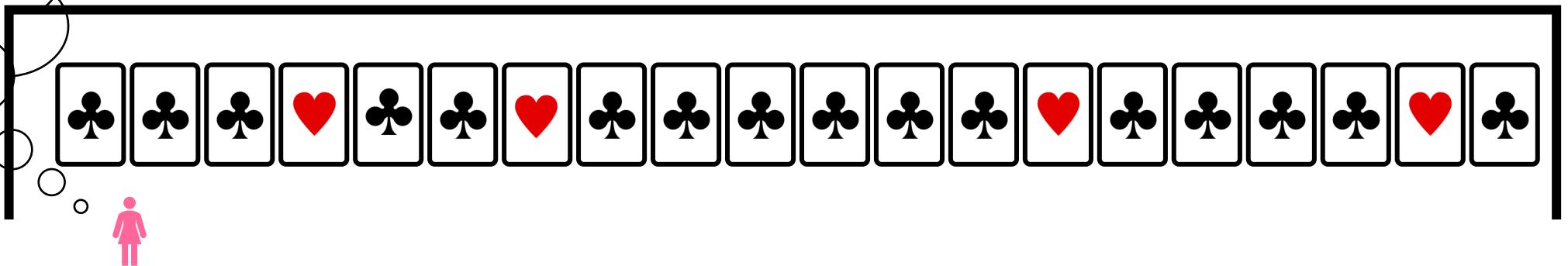


How to secretly select the 4 commitments corresponding to the guess?

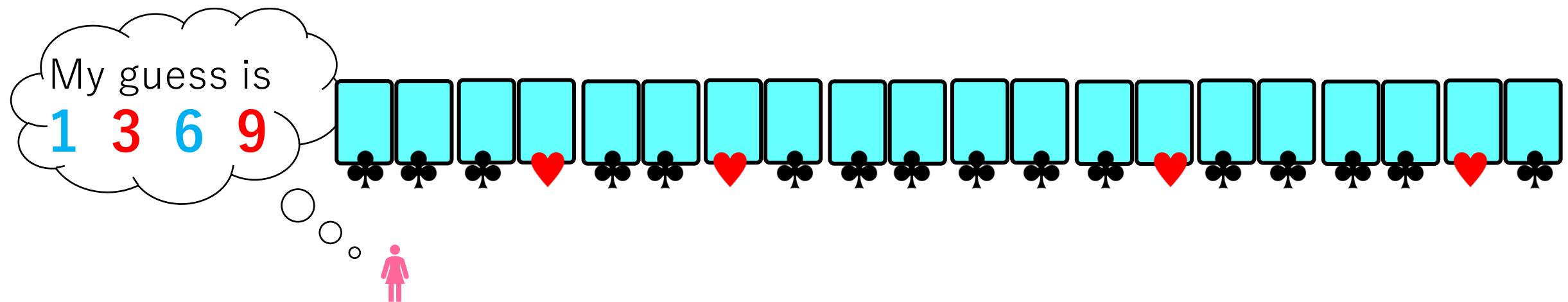
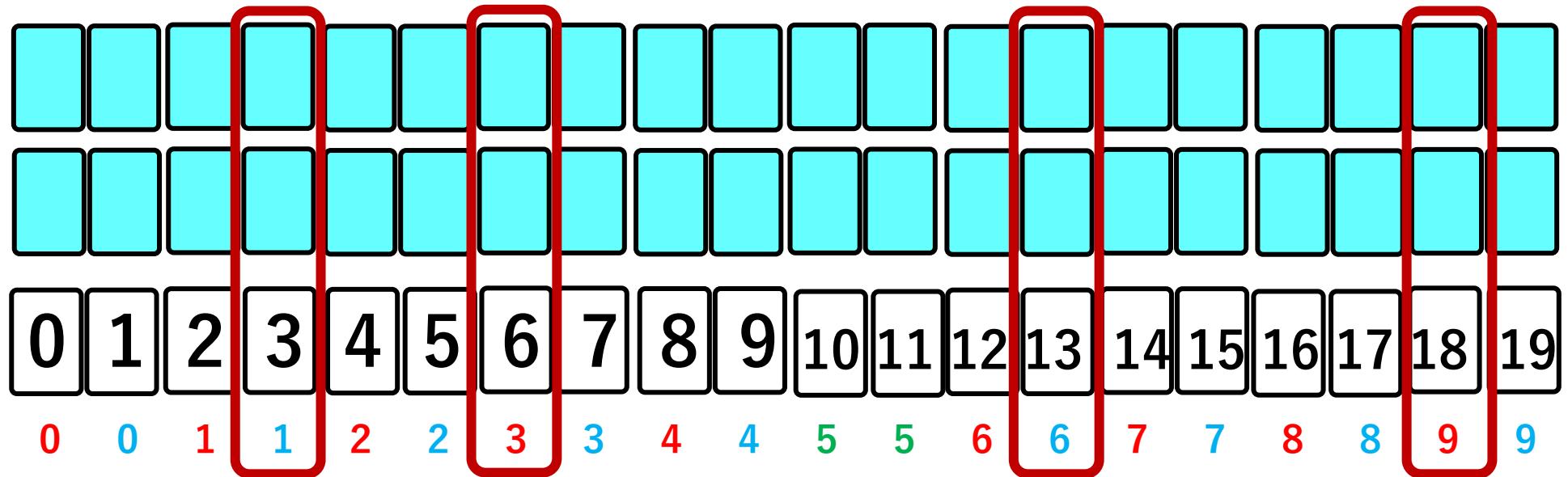
Challenge protocol



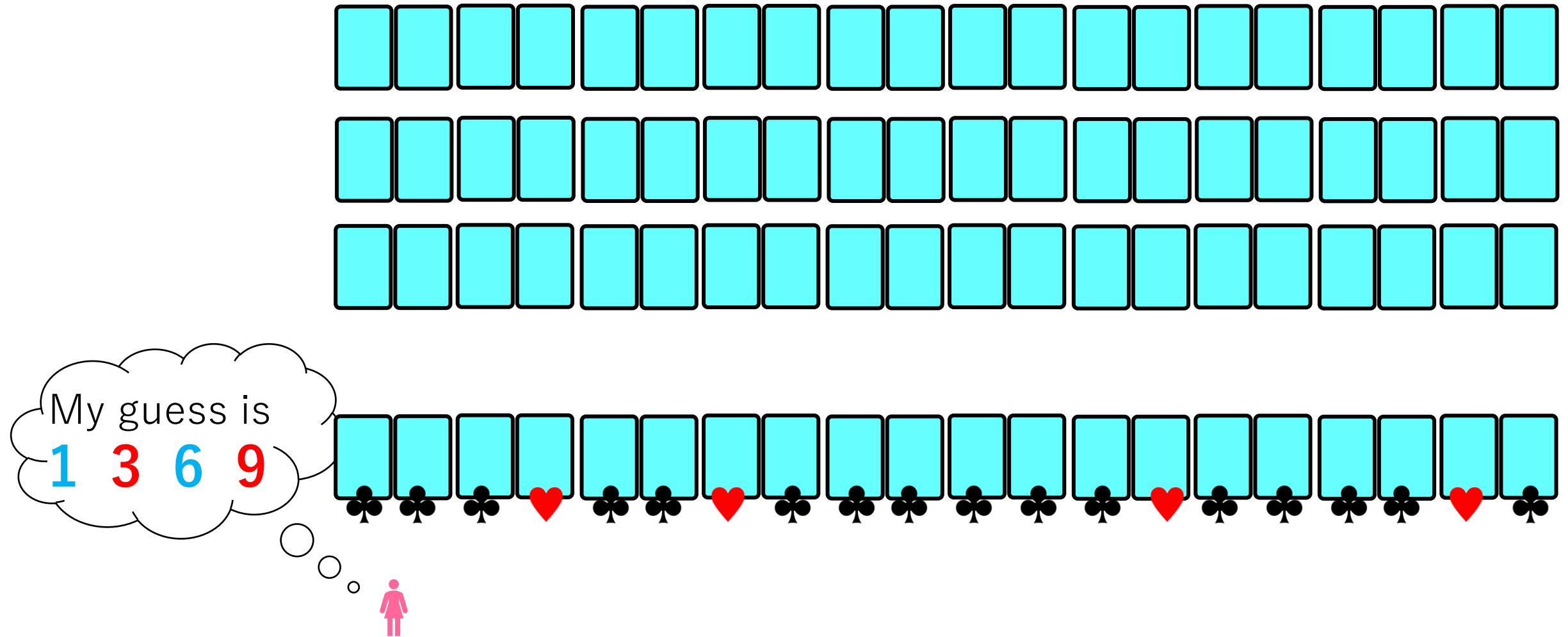
My guess is
1 3 6 9



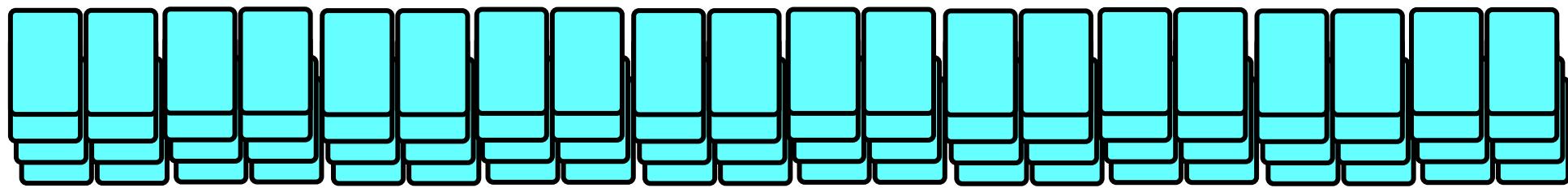
Challenge protocol



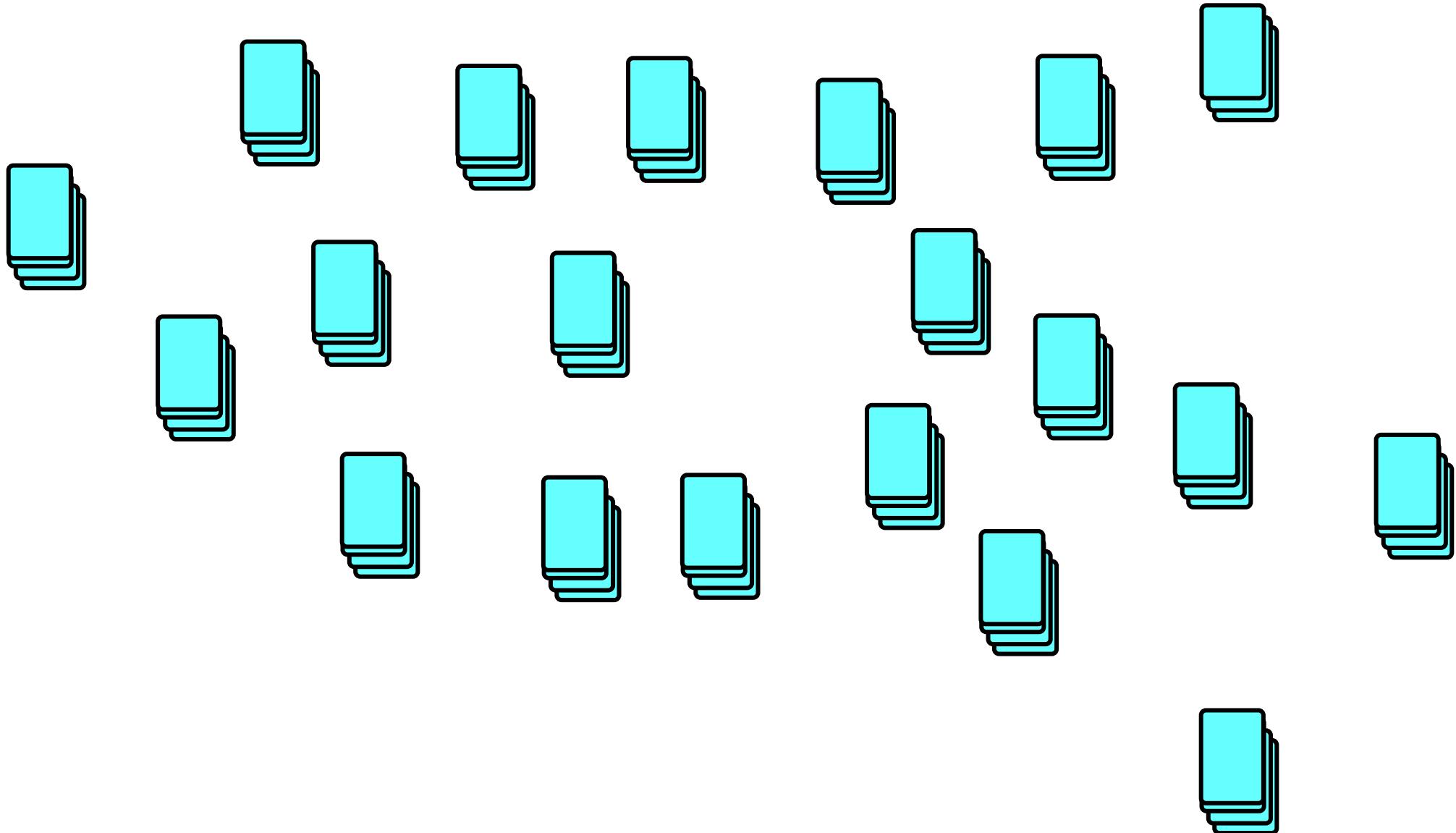
Challenge protocol



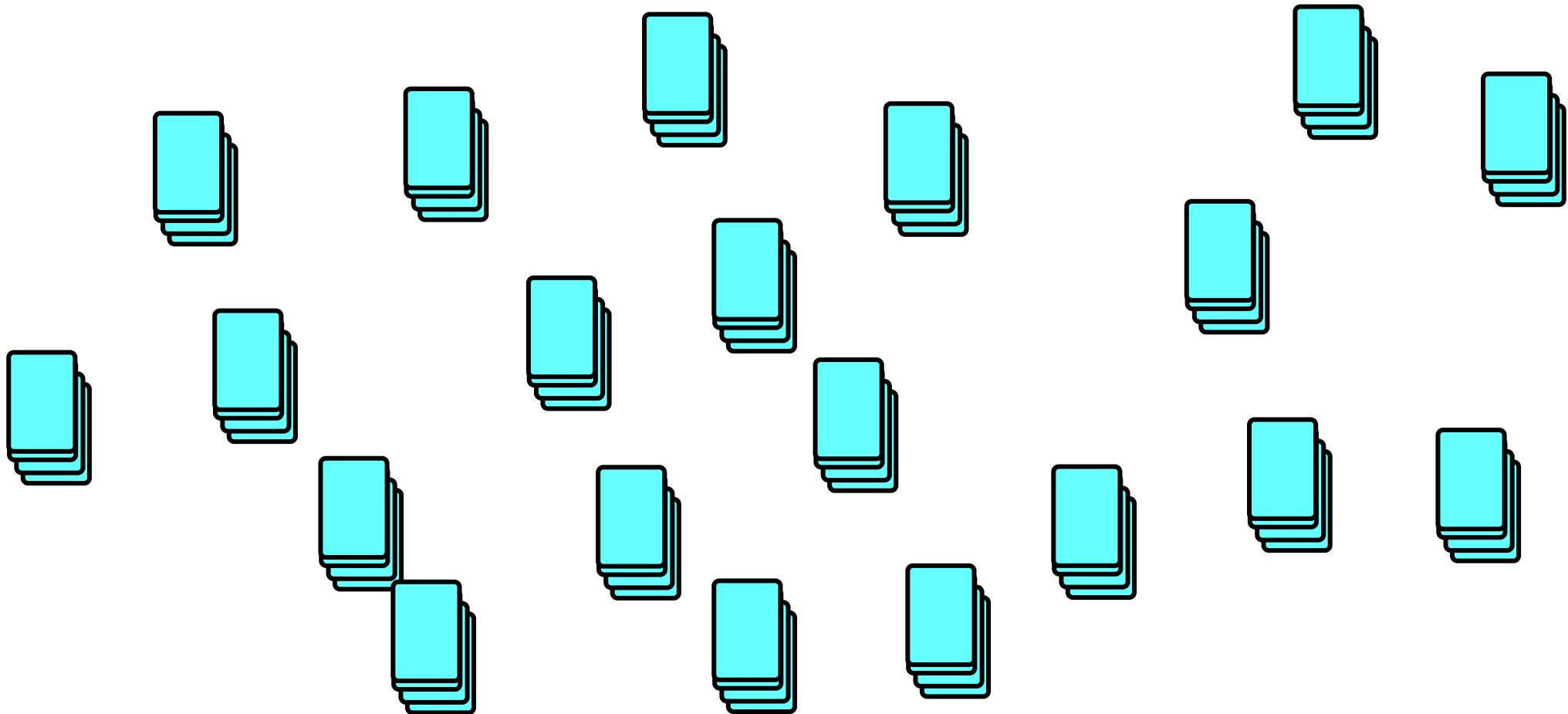
Challenge protocol



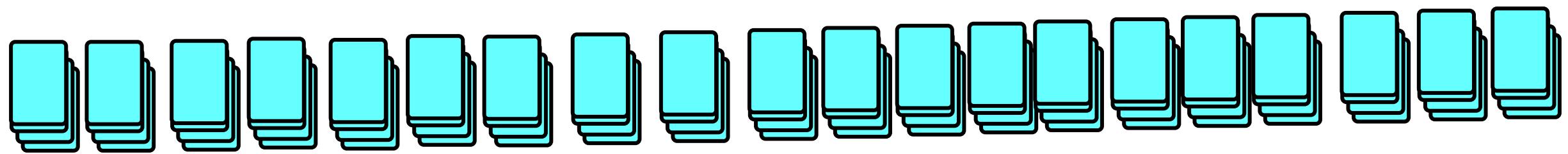
Challenge protocol



Challenge protocol

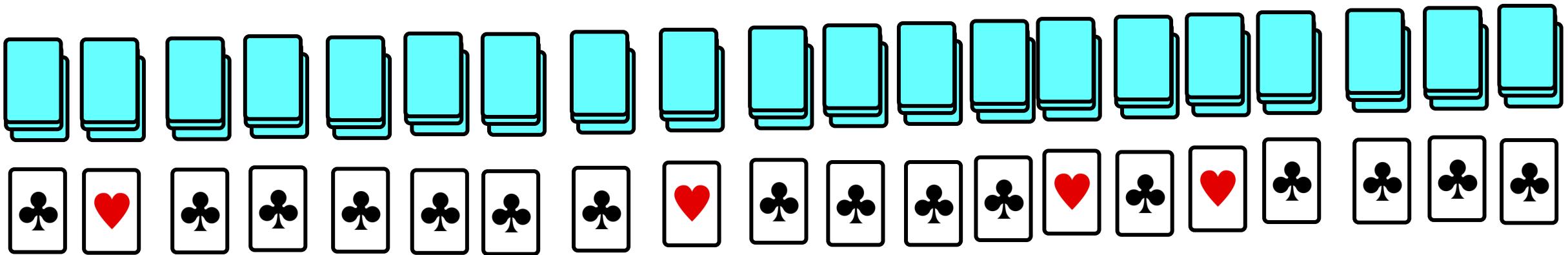


Challenge protocol

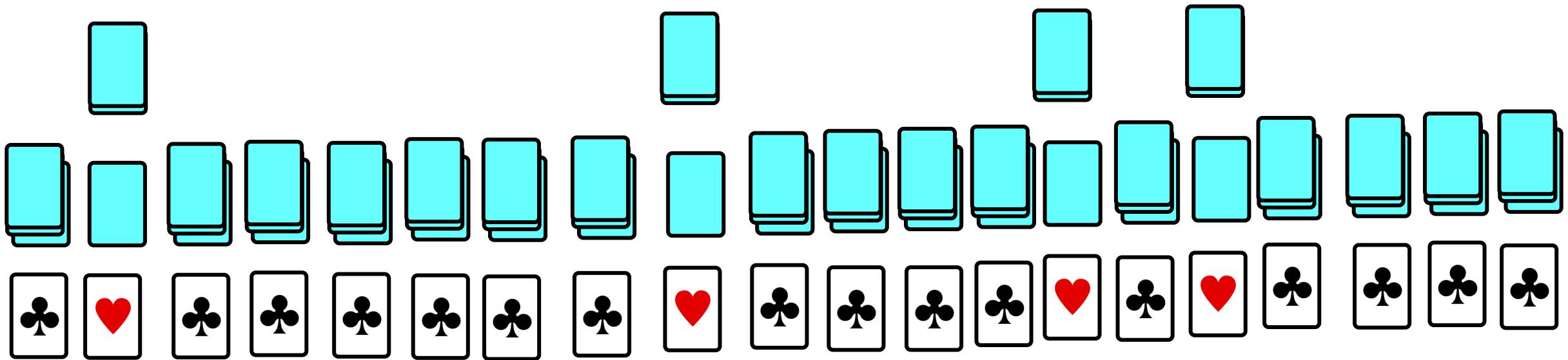


Challenge protocol

Open the bottom cards

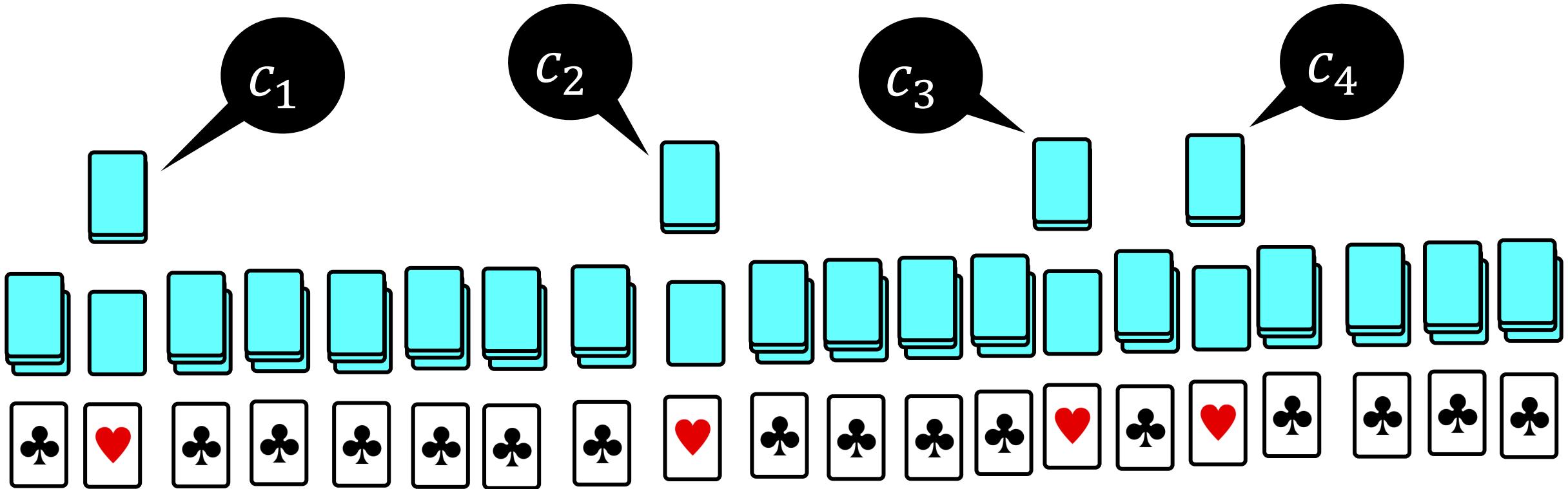


Challenge protocol

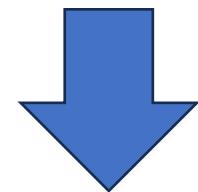
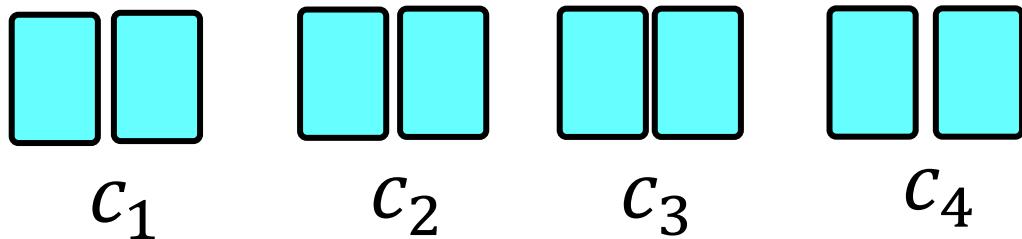


The cards above each  correspond to her guess

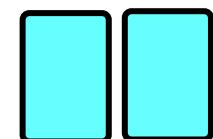
Challenge protocol



Challenge protocol



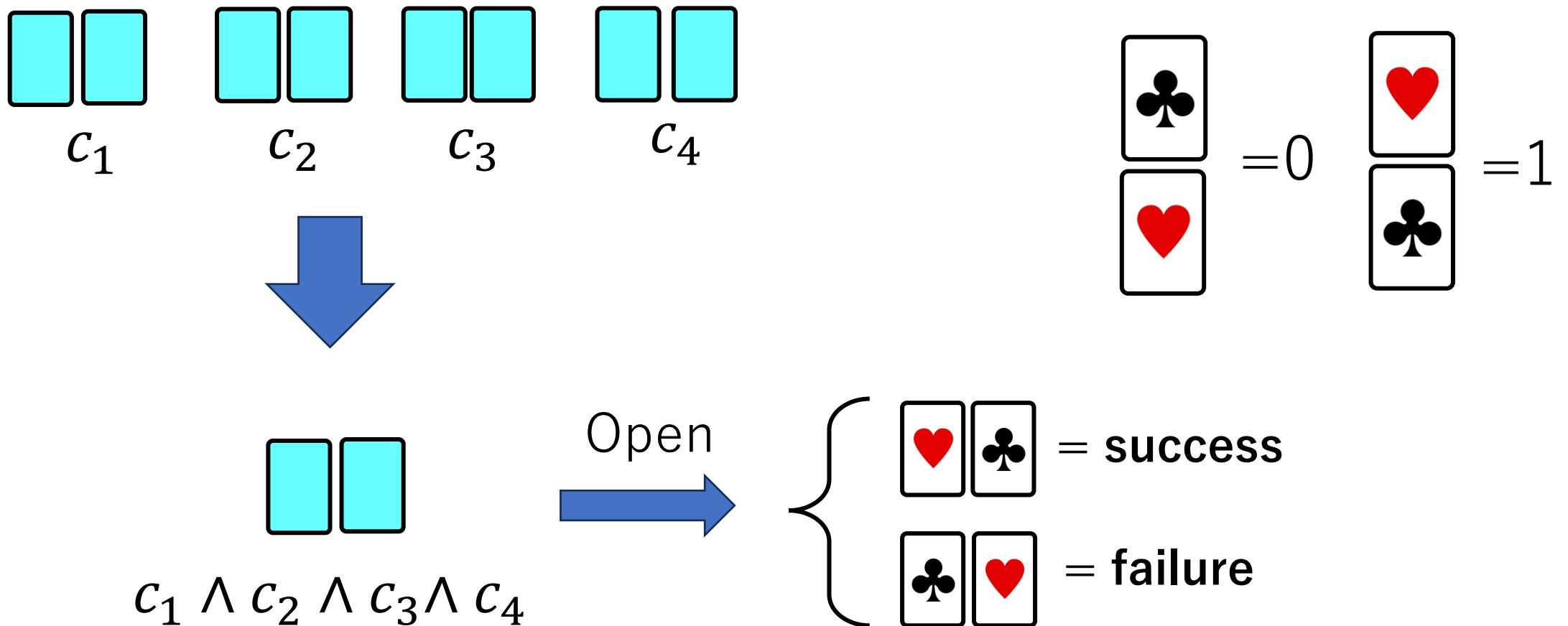
(Variants of) the AND protocol



$c_1 \wedge c_2 \wedge c_3 \wedge c_4$

We also make copies here; see Step 4 in Section 3.3.

Challenge protocol



We can only know whether the challenge succeeds or not

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Conclusion

- We apply card-based cryptography to enhancing the gameplay of Tagiron.
- Useful tool to promote intuitive understanding of secure computations.
- The number of cards used in our method is not small, and further optimization is future work.

